

# Service Engineering & Science: Data-Based Research, Teaching, Practice

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Wharton Empirical OM, September 2006

# Main Messages

1. **Simple Models** at the Service of **Complex Realities**.

**Supported** by a Panorama of Empirical and Theoretical Models.

2. **Data-Based** Analysis is a Must & Fun (after tenure?).

**Supported** by **DataMOCCA** = Data **MO**del for **C**all **C**enter **A**nalysis, initiated at **Wharton**, currently developed at **Technion** and available for adoption.

3. **Back to the Basic-Research Paradigm** (Physics, Biology, . . .):  
**Measure, Model, Experiment, Validate, Refine, etc.**

4. **Ancestors** & **Practitioners** often knew/apply the “**right answer**”:  
simply did/do not have our tools/desire/need to prove it so.

**Supported** by Erlang (1915), Palm (1945),..., seasoned & thoughtful managers.

## Background Material (Downloadable)

- ▶ Technion's "**Service-Engineering" Course** ( $\geq 1995$ ):  
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- ▶ Gans (U.S.A.), Koole (Europe), and M. (Israel):  
"Telephone Call Centers: Tutorial, Review and Research Prospects." MSOM, 2003.
- ▶ Brown, Gans, M., Sakov, Shen, Zeltyn, Zhao:  
"Statistical Analysis of a Telephone Call Center: A Queueing-Science Perspective." JASA, 2005.
- ▶ Trofimov, Feigin, M., Ishay, Nadjharov:  
"DataMOCCA: Models for Call/Contact Center Analysis."  
Technion Report, 2004-2006.
- ▶ M. "Call Centers: Research Bibliography with Abstracts."  
Version 7, December 2006.

# Present Focus: Call Centers, but Expanding

## Call Centers: Business-Frontiers & Sweat-Shops of 21<sup>st</sup> Century

### U.S. Statistics (Relevant Elsewhere)

- ▶ Over 60% of annual business volume via the telephone
- ▶ 70,000 – 200,000 call centers
- ▶ 3 – 6.5 million employees (**3% – 6% workforce**)
- ▶ 20% annual growth rate
- ▶ \$100 – \$300 billion annual expenditures
- ▶ 1000's agents in a "single" call center.

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### Expanding, eg. **Healthcare**:

- ▶ **Similar** Challenges: Scarce transactional data, natural queueing-network view, human-operations interface (**7% LWBS**), nurse-staffing (several millions), ...
- ▶ **Unique** Challenges: More risk, less scale-economies, more synchronization gaps, ...

## The First Prerequisite: Data & Measurements

Empirical “Axiom”: The data one needs is **never** there for one to use – always problems with historical data.

Data at the level of **Individual-Transactions**: Time-Stamps of Events

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Current Databases: **Operations** (vs. Marketing, Surveys, ...)

- ▶ **Face-to-Face** data (bank - bar-code readers): **Recitations**
- ▶ **Telephone** data (small cc - 350K calls/year): **Homework**
- ▶ **DataMOCCA** (large cc's - 350K call/week): **Research**



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**Future Research: - experience anyone?**

- ▶ Healthcare (via RFID)
- ▶ Multimedia: Telephone + email + Internet (log-files)
- ▶ Field-Support
- ▶ Operation + Marketing (ACD + CRM)

# Measurements: Face-to-Face Services

## 23 Bar-Code Readers at a Bank Branch

Bank – 2nd Floor Measurements

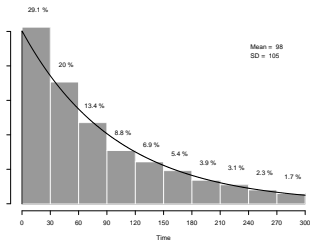


# Measurements: Telephone Call-by-Call Data (Log-File)

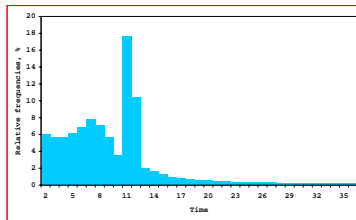
row_id	call_id	customer_id	month	type	date	row_time	q_start	q_end	q_time	outcome	ser_start	ser_end	ser_time	server
AA010 44749 27644400 1 PS 99090 11:45:33 11:45:39 6 11:45:39 11:46:58 79 AGENT 11:46:57 11:51:00 243 DORIT														
AA010 44750 2887816 1 PS 99090 14:49:00 14:49:06 6 14:49:06 14:53:00 234 AGENT 14:52:59 14:54:20 90 ROTH														
AA010 44967 58660291 2 PS 99090 14:58:42 14:58:48 6 14:58:48 15:02:31 223 AGENT 15:02:31 15:04:10 99 ROTH														
AA010 44968 0 0 NW 99090 15:10:17 15:10:26 9 15:10:26 15:13:19 173 HANG 00:00:00 00:00:00 0 NO_SERVER														
AA010 44969 63193346 2 PS 99090 15:22:07 15:22:13 6 15:22:13 15:23:21 68 AGENT 15:23:20 15:25:25 125 STEREN														
AA010 44970 0 0 NW 99090 15:31:33 15:31:47 14 00:00:00 00:00:00 0 AGENT 15:31:43 15:34:16 151 STEREN														
AA010 44971 41630443 2 PS 99090 15:37:29 15:37:34 5 15:37:34 15:38:20 46 AGENT 15:38:18 15:40:56 158 TOVA														
AA010 44972 64185333 2 PS 99090 15:44:32 15:44:37 5 15:44:37 15:47:57 200 AGENT 15:47:56 15:49:02 66 TOVA														
AA010 44973 3106E+08 1 PS 99090 15:53:05 15:53:11 6 15:53:11 15:56:39 208 AGENT 15:56:38 15:56:39 0 MORIAH														
AA010 44974 74709117 2 NE 99090 15:59:34 15:59:40 6 15:59:40 16:02:33 173 AGENT 16:02:33 16:26:04 1411 ELI														
AA010 44975 35920255 2 PS 99090 16:07:46 16:07:51 5 16:07:51 16:08:01 10 HANG 00:00:00 00:00:00 0 NO_SERVER														
AA010 44976 0 0 NW 99090 16:11:38 16:11:48 10 16:11:48 16:11:50 2 HANG 00:00:00 00:00:00 0 NO_SERVER														
AA010 44977 13689787 2 PS 99090 16:14:27 16:14:33 6 16:14:33 16:14:54 21 HANG 00:00:00 00:00:00 0 NO_SERVER														
AA010 44978 23817067 2 PS 99090 16:19:11 16:19:17 6 16:19:17 16:19:59 22 AGENT 16:19:38 16:21:57 139 TOVA														
AA010 44984 0 0 PS 99090 15:03:26 15:03:36 10 00:00:00 00:00:00 0 AGENT 15:03:35 15:06:36 181 ZOHAR														
AA010 44985 25219700 2 PS 99090 15:14:46 15:14:51 5 15:14:51 15:15:10 19 AGENT 15:15:09 15:17:50 111 SHARON														
AA010 44786 0 0 PS 99090 15:25:48 15:26:00 12 00:00:00 00:00:00 0 AGENT 15:25:59 15:28:15 136 ANAT														
AA010 44767 58859752 2 PS 99090 15:34:57 15:35:03 6 15:35:03 15:35:14 11 AGENT 15:35:13 15:31:51 2 MORIAH														
AA010 44768 0 0 PS 99090 15:46:30 15:46:39 9 00:00:00 00:00:00 0 AGENT 15:46:38 15:51:31 813 ANAT														
AA010 44769 78191137 2 PS 99090 15:56:03 15:56:09 6 15:56:09 15:56:28 19 AGENT 15:56:28 15:59:02 154 MORIAH														
AA010 44770 0 0 PS 99090 16:14:31 16:14:46 15 00:00:00 00:00:00 0 AGENT 16:14:44 16:16:02 78 BENSON														
AA010 44771 0 0 PS 99090 16:38:59 16:39:12 13 00:00:00 00:00:00 0 AGENT 16:39:11 16:43:35 264 VICKY														
AA010 44772 0 0 PS 99090 16:51:40 16:51:50 10 00:00:00 00:00:00 0 AGENT 16:51:49 16:53:52 123 ANAT														
AA010 44773 0 0 PS 99090 17:02:19 17:02:28 9 00:00:00 00:00:00 0 AGENT 17:02:28 17:07:42 314 VICKY														
AA010 44774 3287482 1 PS 99090 17:18:18 17:18:24 6 17:18:24 17:19:01 37 AGENT 17:19:00 17:19:35 15 VICKY														
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AA010 44776 0 0 PS 99090 17:52:59 17:53:09 10 00:00:00 00:00:00 0 AGENT 17:53:08 17:53:09 1 NO_SERVER														
AA010 44777 3763590 2 PS 99090 18:15:47 18:15:52 5 18:15:52 18:16:57 65 AGENT 18:16:56 18:18:48 112 ANAT														
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AA010 44782 0 0 NW 99090 20:08:13 20:08:25 12 00:00:00 00:00:00 0 AGENT 20:08:20 20:08:41 13 NO_SERVER														
AA010 44783 0 0 PS 99090 20:23:51 20:24:05 14 00:00:00 00:00:00 0 AGENT 20:24:04 20:24:33 29 BENSON														
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AA010 44787 0 0 PS 99090 21:25:00 21:25:13 13 00:00:00 00:00:00 0 AGENT 21:25:13 21:28:03 170 AVI														
AA010 44788 0 0 PS 99090 21:50:40 21:50:54 14 00:00:00 00:00:00 0 AGENT 21:50:54 21:51:55 61 AVI														
AA010 44789 9103000 2 NE 99090 22:05:40 22:05:46 6 22:05:46 22:09:52 46 AGENT 22:09:51 22:13:41 230 AVI														
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# Beyond Averages: Waiting Times in a Call Center

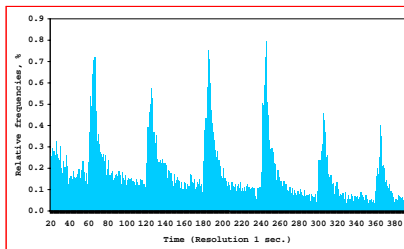
## Small Israeli Bank



## Large U.S. Bank

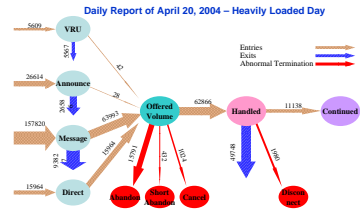


## Medium Israeli Bank

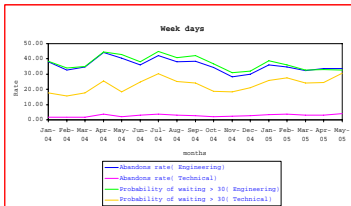


# DataMOCCA = Models for Call Center Analysis

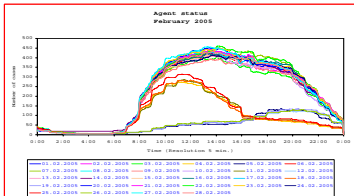
## Daily Report



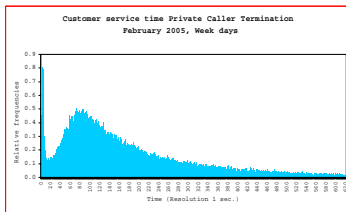
## Time Series



## Cross Tabulation



## Histogram



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Through **Examples** Only.

Each example starts with a **Complex Reality** and ends with a **useful** insight due to a **Simple Model**.

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“**Theorem**”: A useful model must be simple (yet not too simple).

Models in decreasing simplicity-levels:

- ▶ **Conceptual**: Service Networks = **Queueing Networks**
- ▶ **Descriptive**: Averages, Histograms
- ▶ **Explanatory**: Comparative, Regression
- ▶ **Analytical/Mathematical**: Little's Law, Fluid Models, Queueing Models, Diffusion Approximations.

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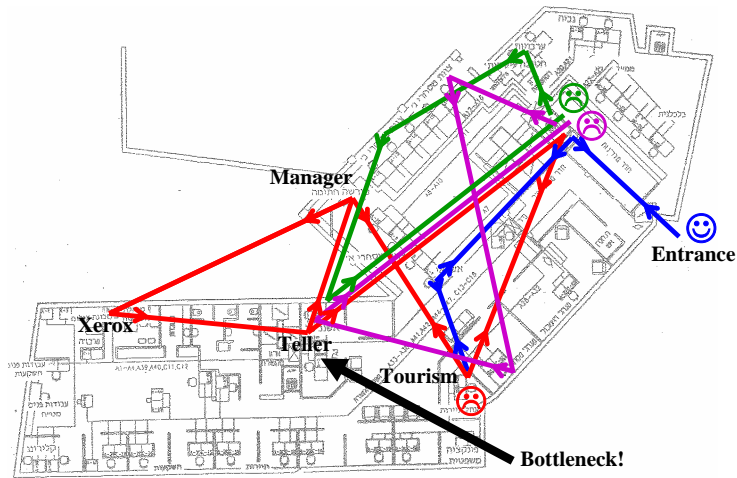
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“**Corollary**”: To be useful, a simple model sometimes requires deep analysis.



# Conceptual Model: Face-to-Face Services

Bank Branch = Queueing Network



# Descriptive Model: Transition Probabilities (Averages)

## Transition Frequencies Between Units in The Private and Business Sections:

		Private Banking				Business				
	To Unit From Unit	Bankers	Authorized Personal	Compens - - ations	Tellers	Tellers	Overdrafts	Authorized Personal	Full Service	Exit
Private Banking	Bankers		1%	1%	4%	4%	0%	0%	0%	90%
	Authorized Personal	12%		5%	4%	6%	0%	0%	0%	73%
	Compensations	7%	4%		18%	6%	0%	0%	1%	64%
	Tellers	6%	0%	1%		1%	0%	0%	0%	90%
Services	Tellers	1%	0%	0%	0%		1%	0%	2%	94%
	Overdrafts	2%	0%	1%	1%	19%		5%	8%	64%
	Authorized Personal	2%	1%	0%	1%	11%	5%		11%	69%
	Full Service	1%	0%	0%	0%	8%	1%	2%		88%
	Entrance	13%	0%	3%	10%	58%	2%	0%	14%	0%

Legend:

0% - 5%	5% - 10%	10% - 15%	>15%
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## Dominant Paths - Business:

Unit Parameter	Station 1 Tourism	Station 2 Teller	Total Dominant Path
Service Time	12.7	4.8	17.5
Waiting Time	8.2	6.9	15.1
Total Time	20.9	11.7	32.6
Service Index	0.61	0.41	0.53

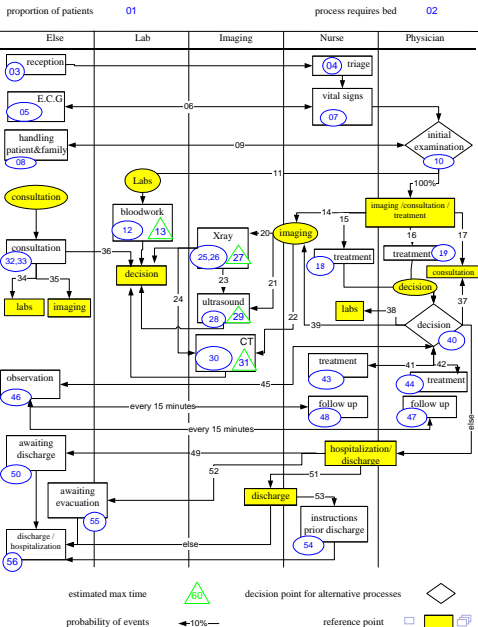
## Mapping the Offered Load (Bank Branch)

Department Time	Business Services		Private Banking	Banking Services	
	Tourism	Teller	Teller	Teller	Comprehensive
8:30 – 9:00	Not Busy	Very Busy	Very Busy	Very Busy	Very Busy
9:00 – 9:30	Not Busy	Not Busy	Not Busy	Not Busy	Not Busy
9:30 – 10:00	Very Busy	Very Busy	Very Busy	Very Busy	Very Busy
10:00 – 10:30	Very Busy	Very Busy	Very Busy	Very Busy	Very Busy
10:30 – 11:00	Very Busy	Very Busy	Very Busy	Very Busy	Very Busy
11:00 – 11:30	Not Busy	Very Busy	Very Busy	Very Busy	Very Busy
11:30 – 12:00	Not Busy	Very Busy	Very Busy	Very Busy	Very Busy
12:00 – 12:30	Not Busy	Not Busy	Not Busy	Not Busy	Not Busy
Break	Not Busy	Not Busy	Not Busy	Not Busy	Not Busy
16:00 – 16:30	Very Busy	Very Busy	Very Busy	Very Busy	Very Busy
16:30 – 17:00	Very Busy	Very Busy	Very Busy	Very Busy	Very Busy
17:00 – 17:30	Very Busy	Very Busy	Very Busy	Very Busy	Very Busy
17:30 – 18:00	Very Busy	Very Busy	Very Busy	Very Busy	Very Busy

Legend:

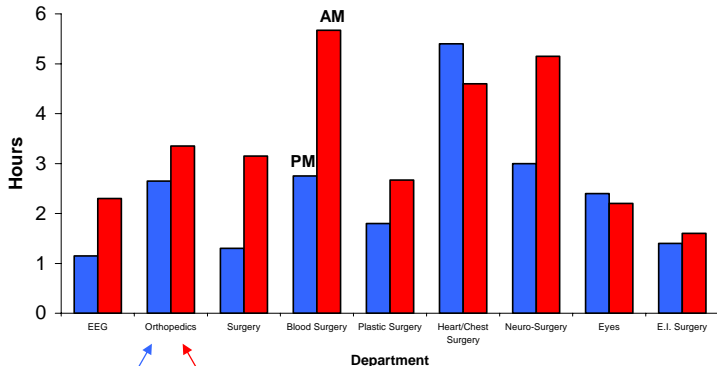
Not Busy	Not Busy
Busy	Busy
Very Busy	Very Busy

# Conceptual Model: Hospital (ED) Network (Sinreich)



# Descriptive Model: Service Times (Averages) or, Even "Doctors" Can Manage

Operations Time - **Morning (by Hour)** vs. **Afternoon (by Case)**:

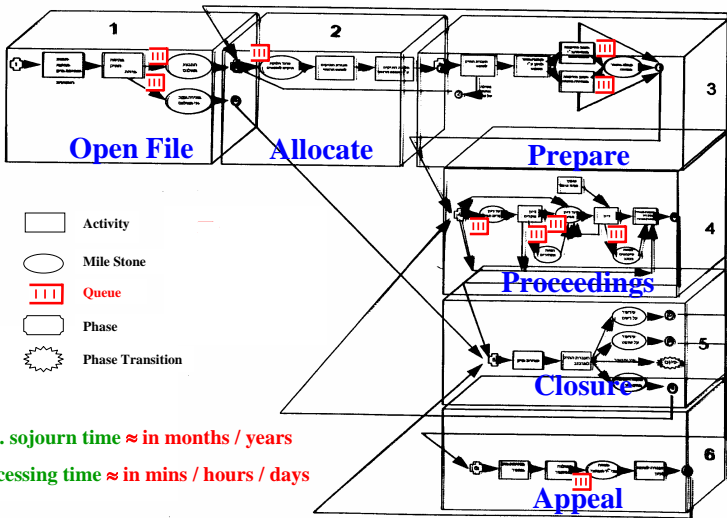


**Afternoon,  
by Case**

**Morning,  
by Hour**

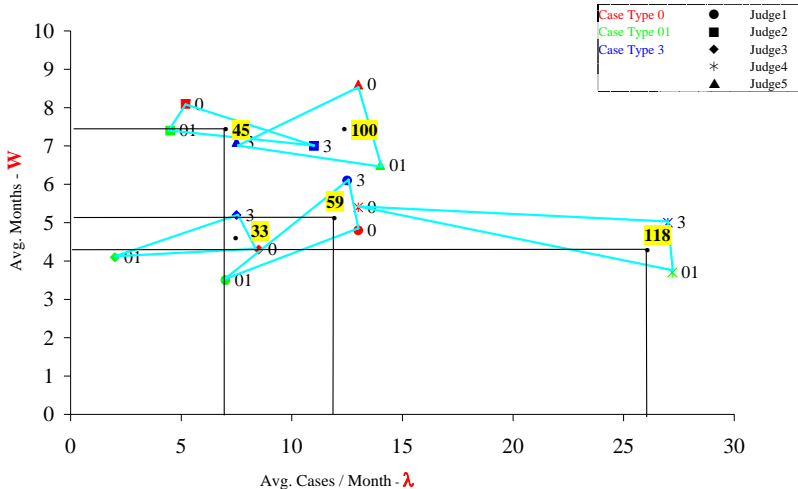
# Conceptual Model: The "Production of Justice"

## The Labor-Court Process in Haifa, Israel



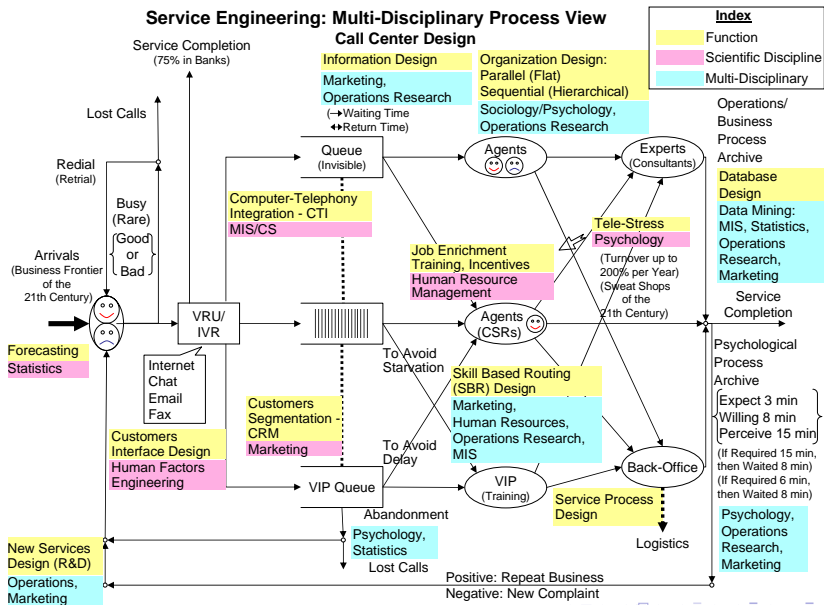
# Analytical Model: Little's Law in Court (still Averages)

## Judges: The Best/Worst (Operational) Performer



# Call-Center Network: Flow, Functions, Disciplines

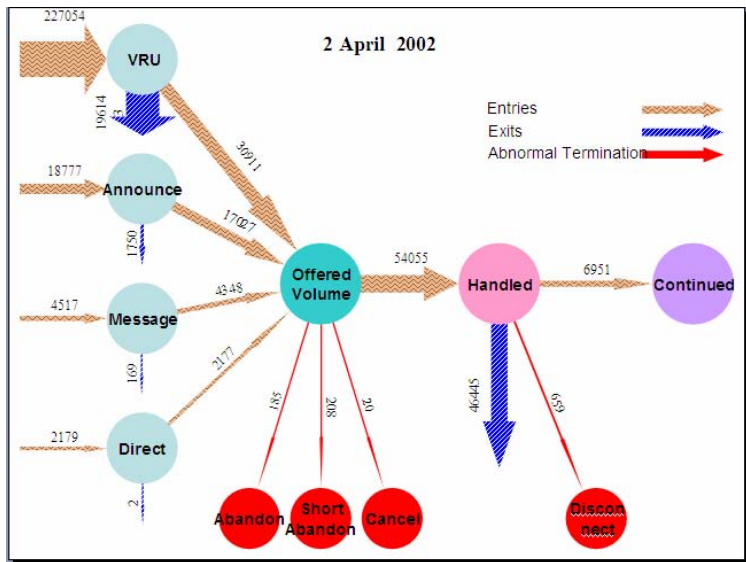
## Service Engineering: Multi-Disciplinary Process View Call Center Design



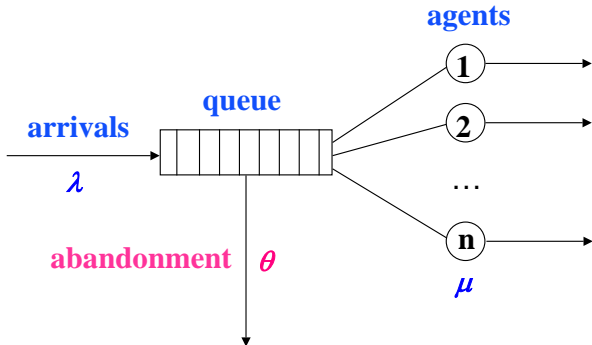


# Conceptual Model: Telephone Service

Call-Center = Queueing-Network (U.S. Bank, via DataMOCCA)



## The Basic Staffing Model: Erlang-A (M/M/n +M)



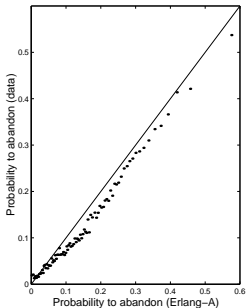
### Erlang-A Parameters:

- ▶  $\lambda$  – **Arrival** rate (Poisson)
- ▶  $\mu$  – **Service** rate (Exponential)
- ▶  $\theta$  – **Impatience** rate (Exponential)
- ▶  $n$  – Number of **Service-Agents**.

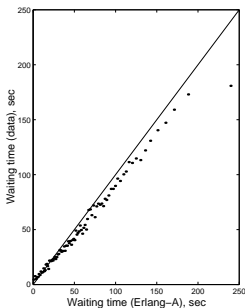
# Erlang-A: Fitting a Simple Model to a Complex Reality

## Hourly Performance vs. Erlang-A Predictions

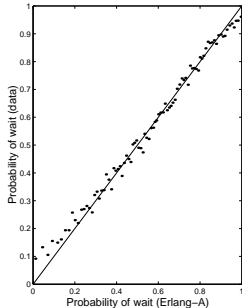
### % Abandon



### $E[Wait]$



### $\% \{Wait > 0\}$

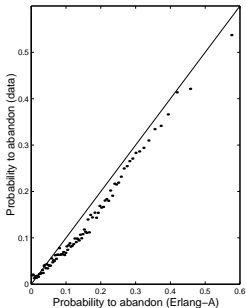


- ▶ Small Israeli bank (10 agents)
- ▶ Empirically-Based Estimation of Patience ( $P\{Ab\}/E[W_q]$ )

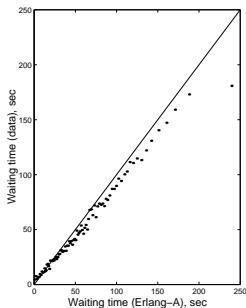
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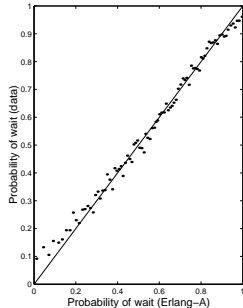
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$E[Wait]$



$\% \{ Wait > 0 \}$



- ▶ Small Israeli bank (10 agents)
- ▶ Empirically-Based Estimation of Patience ( $P\{Ab\}/E[W_q]$ )
- ▶ **Asymptotic formulae fit even better:**
  - Theory** – Why so **Robust** wrt size, features? **Boundaries?**
  - Practice** – eg. few-server time-varying systems (Healthcare, ...)

## Erlang-A: Simple, but Not Too Simple

### Experience:

- ▶ Arrival process **not pure Poisson** (time-varying,  $\sigma^2$  too large)
- ▶ Service times **not exponential** (typically close to lognormal)
- ▶ Patience times **not exponential** (various patterns observed).
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2. Why Stochastic-Ignorant staffing work? Special-Case.
3. How to Accommodate Generalizations? Time-Varying, SBR, ...

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**Answers** via **Asymptotic Analysis**, as load- and staffing-levels  $\uparrow$  :

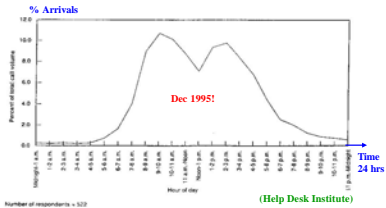
The **QED Regime**, where QED = **Q**uality & **E**fficiency **D**riven.

**Erlang (1915-25)**, **Halfin-Whitt (1981)**; recent surge of research.

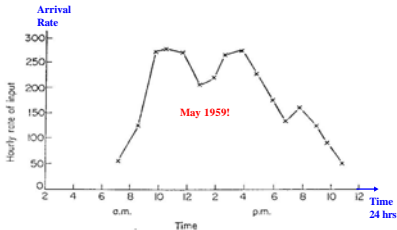
# Arrivals to Service: Poisson-Related

## Arrival Rate to Three Call Centers

December 1995 (U.S. Helpdesks)



May 1959 (England)



November 1999 (Israel)



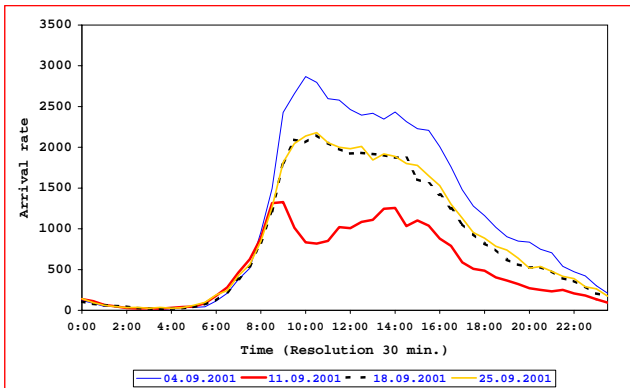
Observation:

**Peak Loads at 10:00 & 15:00**



## Arrivals: Still Poisson-Related, but ...

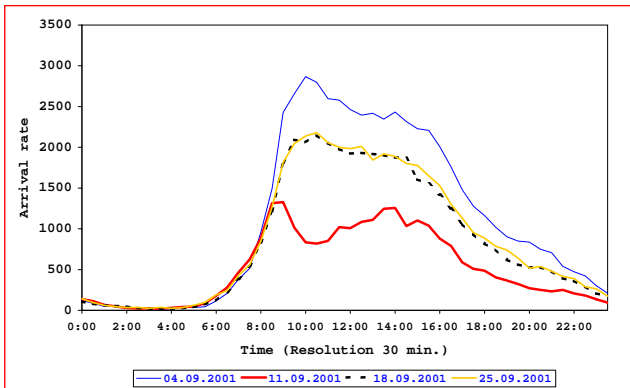
### Arrival Rates on Tuesdays in a September – U.S. Bank



- ▶ **Tuesday**, September 4th: **Heavy**, following Labor Day.
- ▶ **Tuesdays**, September 18, 25: **Normal**.

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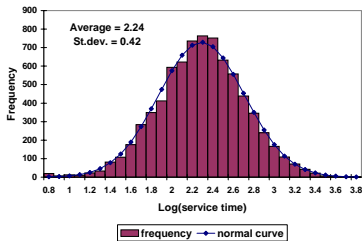
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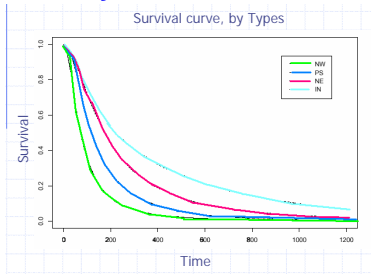
- ▶ **Tuesday**, September 4th: **Heavy**, following Labor Day.
- ▶ **Tuesdays**, September 18, 25: **Normal**.
- ▶ **Tuesday, September 11th, 2001**

# Service Durations: LogNormal Prevalent

## Israeli Bank Log-Histogram



## Survival-Functions by Service-Class



- ▶ **New Customers:** 2 min (NW);
- ▶ **Stock:** 4.5 min (NE);
- ▶ **Regulars:** 3 min (PS);
- ▶ **Tech-Support:** 6.5 min (IN).

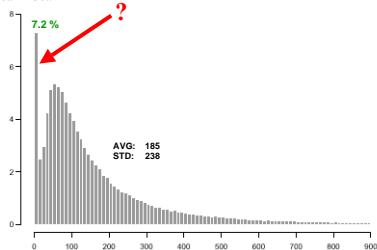
Observation: **VIP** require **longer service** times.

# Service Durations: Still LogNormal, but ...

## Service Times in a Typical (?) Call Center

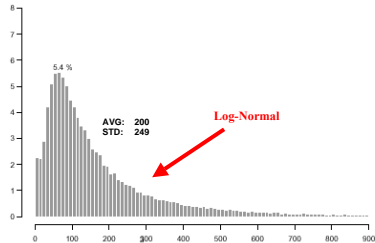
January-October

Jan - Oct:



November-December

Nov - Dec:



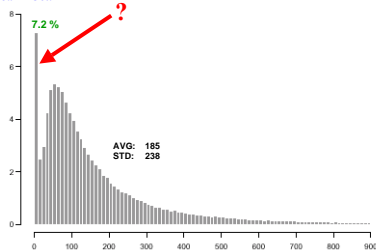
- ▶ **Lognormal** service times are prevalent in call centers.

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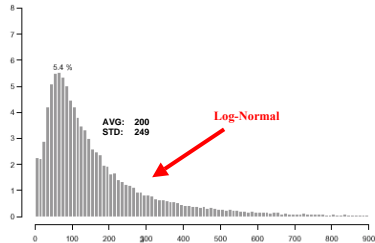
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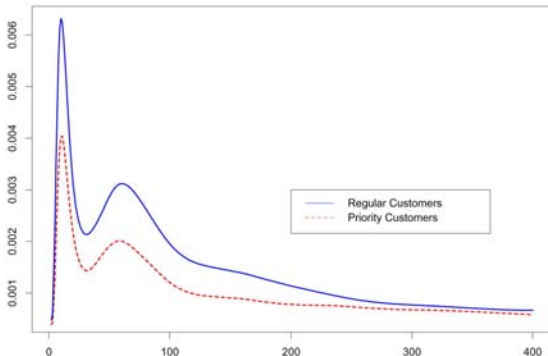
Nov - Dec:



- ▶ **Lognormal** service times are prevalent in call centers.
- ▶ **7.2% Short-Services:** Agents “abandon” (improve bonus, rest).
- ▶ **Distributions**, not only **averages**, must be measured.

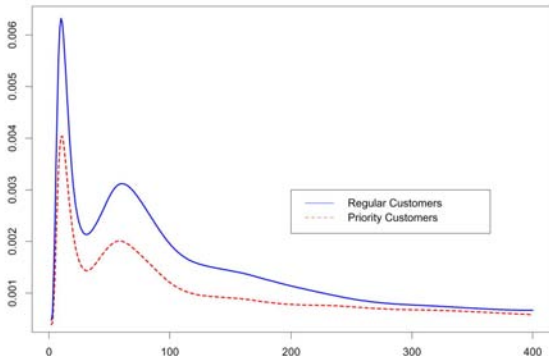
## (Im)Patience while Waiting (Palm 1943-53)

Irritation  $\propto$  Hazard Rate of (Im)Patience Distribution  
Regular over VIP Customers – Israeli Bank



## (Im)Patience while Waiting (Palm 1943-53)

Irritation  $\propto$  Hazard Rate of (Im)Patience Distribution  
**Regular** over **VIP** Customers – Israeli Bank



- ▶ **Peaks** of abandonment at times of **Announcements**
- ▶ **Call-by-Call Data (DataMOCCA)** required (+Censoring).

Observation: **VIP** are **more patient** (Needy)

## Erlang-A: Simple, Useful, Robust, Insightful, Optimal

- ▶ **Simple:** 4CallCenters calculator (download in our Website)
- ▶ **Useful:** Is replacing Erlang-C as the WFM standard
- ▶ **Robust:** QED asymptotics (moderate-to-large systems)
- ▶ **Insightful:** Square-Root Staffing rules; EOS
- ▶ **Optimal:** Could save significant \$'s



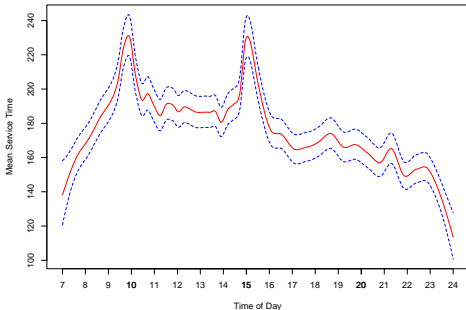
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- ▶ **Optimal:** Could save significant \$'s
- ▶ **and Generalizable:** Time-Varying, CRM/SBR, . . . ,  
still has its **Boundaries**, both Theoretical and Practical:  
  
⇒ **Current Research**

# A "Service-Time" Puzzle at a Small Israeli Bank

## Inter-related Building Blocks

### Average Service Time over the Day – Israeli Bank

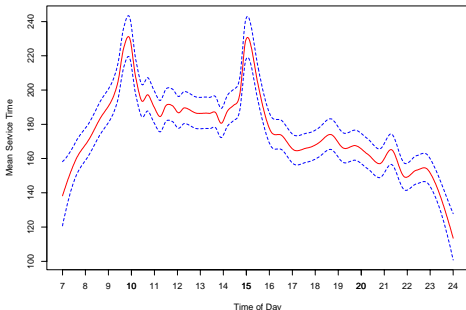


Prevalent: **Longest services at peak-loads (10:00, 15:00). Why?**

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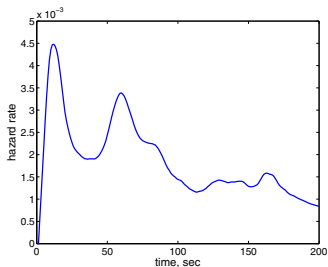
#### Explanations:

- ▶ Prevalent: Service protocol different (longer) at congestion.
- ▶ Operational: The **needy** abandon less during peak loads; hence the **VIP** remain on line, with their **longer** service times.

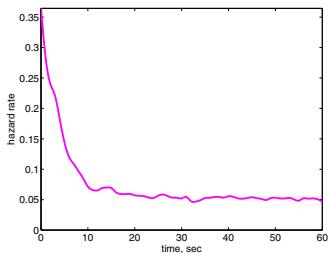
# Call Center Data: Hazard Rates (Un-Censored)

## (Im)Patience Time

Israel



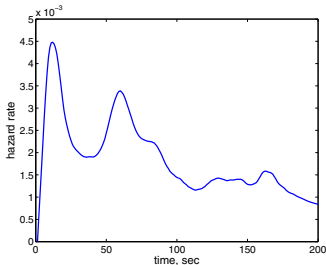
U.S.



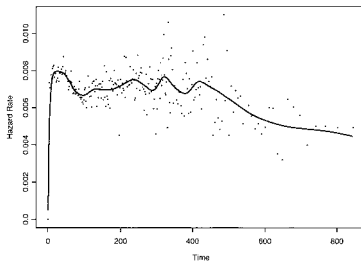
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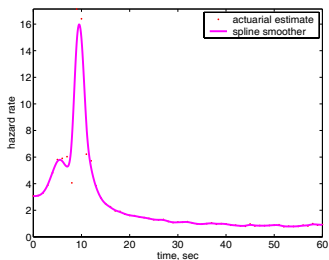
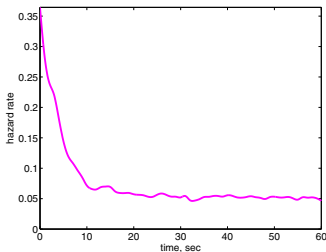
Israel



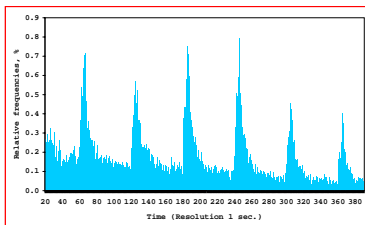
## Required/Offered Wait



U.S.



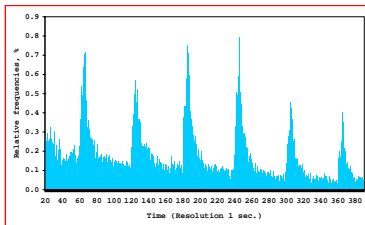
# A “Waiting-Times” Puzzle at a Medium Israeli Bank



## Peaks Every 60 Seconds. Why?

- ▶ Human: **Voice-announcement** every 60 seconds.
- ▶ System: **Priority-upgrade** (unrevealed) every 60 seconds.

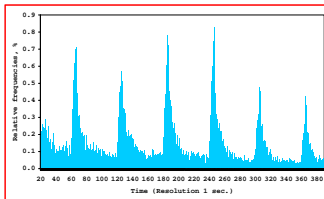
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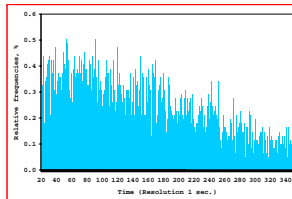
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### Served Customers



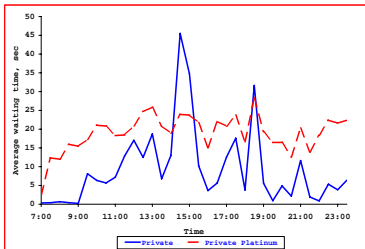
### Abandoning Customers



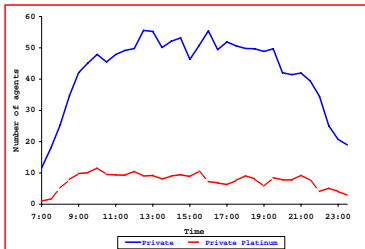
# Priorities and Economies-of-Scale

## Regular vs. VIP Customers: Cellular – March 23, 2004

### Average Wait



### Staffing Level



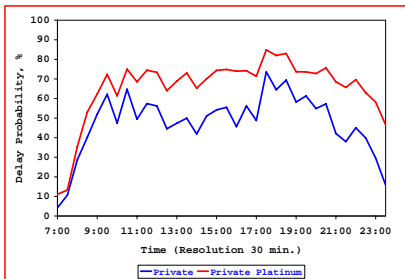
- ▶ **Design:** VIP-dedicated agents, Regular-dedicated Agents.
- ▶ **VIP's** are **not** served better than **Regular's**
- ▶ **Solutions:** Add VIP agents (costly), or Change Design.



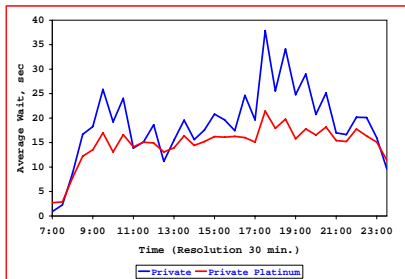
# Priorities and Routing Protocols I

## Regular vs. VIP Customers: Cellular – October 2004

### Delay Probability



### Average Wait



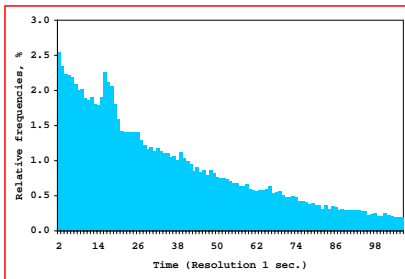
More **VIP's** delayed than **Regular's**, yet their average wait is shorter.

What changed since last March?

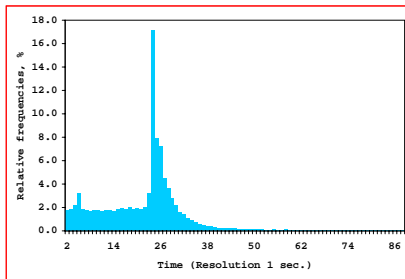
## Priorities and Routing Protocols II

### Waiting-Time Histograms: Cellular – October 2004

Regular Customers



VIP (Platinum) Customers



After **25 seconds** of wait, **VIP** customers are **routed** with **high priority** to Regular agents. Hence, almost **no long waiting times** for VIP's.

## Main Challenges for Research & Practice

- ▶ **Uncertainty:** in Reality, Model Parameters; Forecasting.
- ▶ **Skills-Based Routing:** Convergence of Practice and Theory.
- ▶ **Time-Varying Queues:** Time-Stable Performance.
- ▶ **General Service-Times:** Theory.
- ▶ **Economic Models:** Operations (Dimensioning), Marketing. Refine, etc.

All of the above in a **Network** of distributed call centers.

But there is much more: The **Psychology-Operations** Interface.

Consider, as only one example, the "Phases of Waiting" for Service.

## The "Phases of Waiting" for Service

Common Experience:

- ▶ Expected to wait 5 minutes, Required to 10
- ▶ Felt like 20, Actually waited 10 (hence Willing  $\geq$  10)

An attempt at "Modeling the Experience":

1. Time that a customer **expects** to wait
2. **willing** to wait ((Im)Patience:  $\tau$ )
3. **required** to wait (Offered Wait:  $V$ )
4. **actually** waits ( $W_q = \min(\tau, V)$ )
5. **perceives** waiting.

**Experienced** customers  $\Rightarrow$  Expected = Required  
**Rational** customers  $\Rightarrow$  Perceived = Actual.

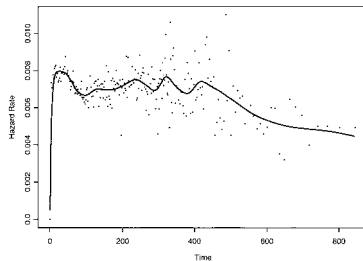
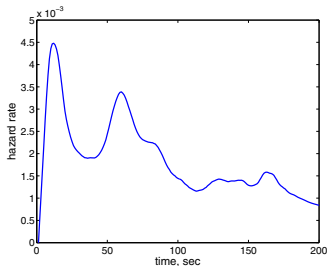
Then left with  $(\tau, V)$ .

# Call Center Data: Hazard Rates (Un-Censored)

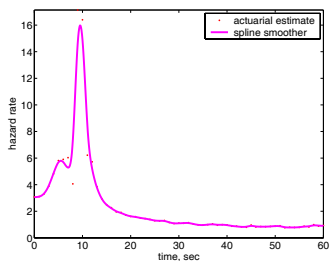
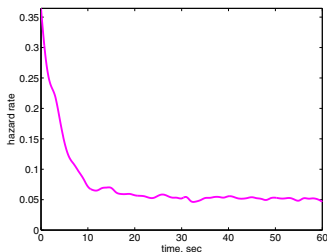
## (Im)Patience Time

## Required/Offered Wait

Israel



U.S.



# A Patience Index

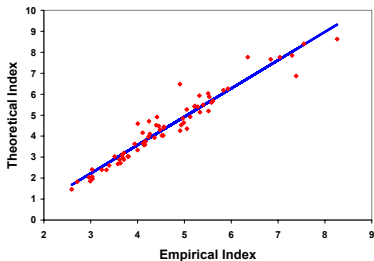
## How to quantify (Im)Patience?

$$\text{Theoretical Patience Index} \triangleq \frac{\text{Willing to wait}}{\text{Expected to wait}} = \frac{E[\tau]}{E[V]},$$

the last = if Experienced: then calculable but complex, error-prone.  
Simple (but not too simple) model suggests the easily-measurable:

$$\text{Empirical Patience Index} \triangleq \frac{\% \text{ Served}}{\% \text{ Abandoning}}$$

## Patience Index – Empirical vs. Theoretical (Brown)



# Predicting Performance

Model **Primitives**:

- ▶ Arrivals to service
- ▶ (Im)Patience while waiting  $\tau$
- ▶ Service times
- ▶ Number of Agents.

Model **Output**: **Offered-Wait  $V$**

Operational Performance Measure calculable in terms of  $(\tau, V)$ .

- ▶ eg. Average Wait =  $E[\min\{\tau, V\}]$
- ▶ eg. % Abandonment =  $P\{\tau < V\}$

**... , and we are back to Erlang-A and relatives, but with lots that's left to do,**

which is comforting.

# DataMOCCA = Data MOdel for Call Center Analysis

**Project Goal:** Designing and Implementing a (universal) data-base/data-repository and interface for storing, retrieving, analyzing and displaying **Call-by-Call-Data**.

## System Components:

- ▶ Clean **Databases**: operational-data of individual calls, agents and operations.
- ▶ Friendly yet powerful **Online Interface**: enables convenient fast access to (mostly) operational and (some) administrative data (but no marketing/business data).

## Current Databases:

- ▶ Medium-sized U.S. Bank (**2.5 years; 220M calls, 40M via agents; 800 agents at peaks**) – Completed.
- ▶ Israeli Cell-Phone Company (**2 years; 110M calls, 25M via agents; 700 agents at peaks**) – Ongoing.
- ▶ Large Israeli Bank – Pilot.