

Skills-Based Routing and its Operational Complexities

Service Engineering

Wharton's Call Center Forum

May 9, 2003

e.mail : avim@tx.technion.ac.il

Website: [http://ie.technion.ac.il/serveng\(2003\)](http://ie.technion.ac.il/serveng(2003))

Tool : <http://4CallCenters.com> (register & use)

Supporting Material (in Web-Site)

Gans, Koole, and M.: “Telephone Call Centers: [Tutorial, Review and Research Prospects.](#)” Invited review to *MSOM*, 2002

Garnett and M.: "An [Introduction](#) to Skills-Based Routing and its Operational Complexities", Teaching Note, 2000; under revision.

Borst, M. and Reiman: “Dimensioning Large Telephone Call Centers.” Accepted to *OR*, 2002.

Atar, M. and Reiman: “Scheduling a Multi-Class Queue with Many Exponential Servers: Asymptotic Optimality in Heavy-Traffic.” Submitted to *Annals Appl Prob*, 2002.

M. and Stolyar: “Scheduling Flexible Servers with Convex Delay Costs: Heavy-Traffic Optimality of the Generalized $c\mu$ -Rule.” Under revision to *OR*, 2002.

Yahalom and M.: "Optimal Scheduling for a Multi-server Multi-class Non-preemptive Queueing System", in preparation.

Armony and M.: "Optimal Routing, Staffing and Networking in the QED (Halfin-Whitt) Regime: Homogenous Customers and Heterogeneous Servers", in preparation.

Contents

1. Introduction to Skills-Based-Routing (SBR):

Examples: CRM, Distributed Call Centers

Truly a Multi-Disciplinary Challenge

2. Focus: Agent Scheduling, Customer Routing and some

Workforce Management (Staffing)

3. Operational Regimes: Quality-Driven, Efficiency-Driven

QED (Quality and Efficiency Driven; Haflin-Whitt)

4. Square-Root Staffing Laws: Scale Economies (Erlang)

5. Efficiency-Driven SBR: Index strategies in the General Case

6. QED SBR: Only special Cases (I, N, V, Upside-Down V)

7. Beyond Conventional Queueing Theory:

Abandonment, Retrials; Time-Varying Queues

Service Engineering – a Subjective View

- Contrast with the traditional and prevalent
 Service Management (Business Schools; U.S.A.)
 Industrial Engineering (Engineering Schools; Europe)
- Goal: Develop scientifically-based design principles (rules-of-thumb) and tools (software), that support the balance of service quality and efficiency, from the (often conflicting) views of customers, servers and managers.
- Theoretical Framework: Queueing Networks
- Applications focus: Call (Contact) Centers

Example: Skills-Based Routing in multi-media centers

e.g. Support + Sales via Telephone + IVR + e.mail + Chat, for VIP and others.

Example: Staffing the modern Call Center

e.g. How many agents to balance service- and efficiency-levels.

Significant: scientific, economic, social, psychological.

Multi-Disciplinary: typically OR/OM, Marketing, HRM. MIS.

The logo for e.b. GEN, featuring the text "e.b." in a stylized font with a red dot, and "GEN" in a bold, black, sans-serif font. The logo is set against a dark background with a grid pattern.

BusinessWeek

A PUBLICATION OF THE MCGRAW-HILL COMPANIES

How to avoid a big tax bill



Will tech's slide keep spreading?

The search for new business models



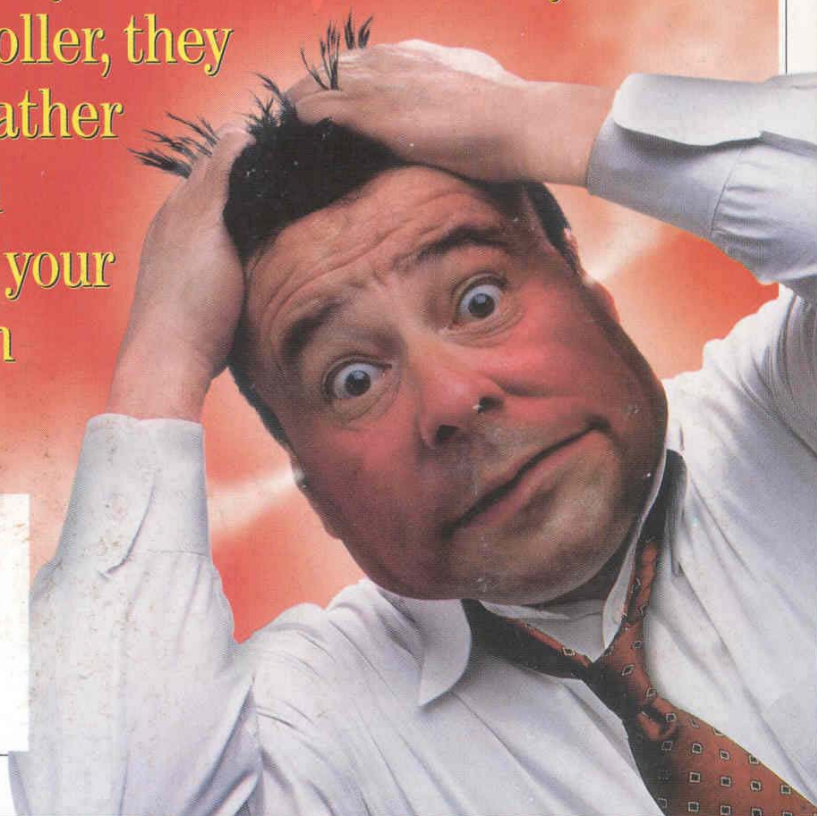
Employers seek a new solution

WHY SERVICE STINKS

Companies know just how good a customer you are – and unless you're a high roller, they would rather lose you than fix your problem

#BXBBGDD****CAR-RT SORT**B083
|||||
#06032865631763#J010201 018489
52/INDUSTRIAL 0830
ENGINEERING LIBRARY 103
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BIRMINGHAM AL 35283-0657

AOL Keyword: BW



Common Performance

BCMS SKILL REPORT

Switch Name: FDC/HAMPDEN

Skill: 37

Skill Name: !BA AUTH1

Date: 7:00 pm WED MAR 10, 1999

Acceptable Service Level: 30

DAY	ACD CALLS	AVG SPEED ANS	ABAND CALLS	AVG ABAND TIME	AVG TALK TIME	TOTAL AFTER CALL	FLOW IN	FLOW OUT	TOTAL AUX/ OTHER	AVG STAFF	% IN SERV LEVL
3/04/99	637	0:19	219	0:26	1:57	92:05	0	0	4310:06	8.7	66
3/05/99	849	0:06	135	0:06	1:35	179:58	0	0	4299:43	11.3	85
3/06/99	1330	0:11	363	0:13	1:42	280:22	0	0	5592:29	13.2	73
3/07/99	1213	0:12	358	0:18	1:46	226:20	0	0	4830:15	11.5	72
3/08/99	631	0:26	382	0:33	1:57	150:50	0	0	3743:04	7.9	49
3/09/99	570	0:40	487	0:43	1:52	148:41	0	0	3979:04	6.7	38
3/10/99	512	0:29	292	0:28	1:41	243:06	0	0	3046:00	7.9	50
SUMMARY	5742	0:18	2236	0:26	1:46	1321:22	0	0	****:**	9.6	63

Arrivals

Abandons 40%

Switch Name: FDC/HAMPDEN

Skill: 46

Skill Name: !BA AUTHORIZATION

Date: 7:00 pm WED MAR 10, 1999

Acceptable Service Level: 30

DAY	ACD CALLS	AVG SPEED ANS	ABAND CALLS	AVG ABAND TIME	AVG TALK TIME	TOTAL AFTER CALL	FLOW IN	FLOW OUT	TOTAL AUX/ OTHER	AVG STAFF	% IN SERV LEVL
3/04/99	1185	0:22	479	0:31	2:08	190:16	0	0	4213:22	8.4	61
3/05/99	1805	0:05	308	0:04	1:38	337:20	0	0	4299:43	11.3	84
3/06/99	2437	0:12	642	0:12	1:51	444:03	0	0	5592:29	13.2	73
3/07/99	2260	0:13	558	0:14	1:46	326:33	0	0	4830:14	11.5	74
3/08/99	1260	0:35	676	0:28	2:06	308:19	0	0	3743:04	7.9	48
3/09/99	1126	0:40	653	0:34	2:10	250:40	0	0	3979:04	6.7	44
3/10/99	890	0:30	472	0:32	2:16	162:13	0	0	3046:00	7.9	51
SUMMARY	10963	0:19	3788	0:22	1:55	2019:24	0	0	****:**	9.6	65

30%

BCMS SKILL REPORT

Switch Name: FDC/HAMPDEN

Skill: 33

Skill Name: GA Authorization

Date: 7:01 pm WED MAR 10, 1999

Acceptable Service Level: 30

DAY	ACD CALLS	AVG SPEED ANS	ABAND CALLS	AVG ABAND TIME	AVG TALK TIME	TOTAL AFTER CALL	FLOW IN	FLOW OUT	TOTAL AUX/ OTHER	AVG STAFF	% IN SERV LEVL
3/04/99	1248	0:27	61	0:42	1:57	330:04	0	0	4390:04	9.5	72
3/05/99	1521	0:14	37	0:20	1:58	353:48	0	0	6035:35	13.0	85
3/06/99	2388	0:20	130	0:34	2:10	550:16	0	0	6369:58	14.4	76
3/07/99	1748	0:14	66	0:30	2:08	432:16	0	0	4616:11	11.7	82
3/08/99	925	0:18	50	1:00	1:53	191:06	0	0	3835:19	8.4	81
3/09/99	856	0:26	57	0:53	1:54	125:16	0	0	4388:02	8.1	73
3/10/99	959	1:15	125	1:55	1:48	186:44	0	0	4198:39	8.9	53
SUMMARY	9645	0:25	526	0:57	2:02	2169:30	0	0	****:**	10.6	76

6%

BCMS SKILL REPORT

Switch Name: FDC/HAMPDEN

Date: 7:02 pm WED MAR 10, 1999

NationsBank CRM:

What are the relationship groups?

- The groups
 - RG1 : high-value customers
 - RG2 : marginally profitable customers (with potential)
 - RG3 : unprofitable customer
- What does it mean for a customer in each group to be **profitable**? Customer **Revenue** Management

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NationsBank's Design of the Service Encounter

Examples of Specifications: [Assignable Grade Of Service \(AGOS\)](#)

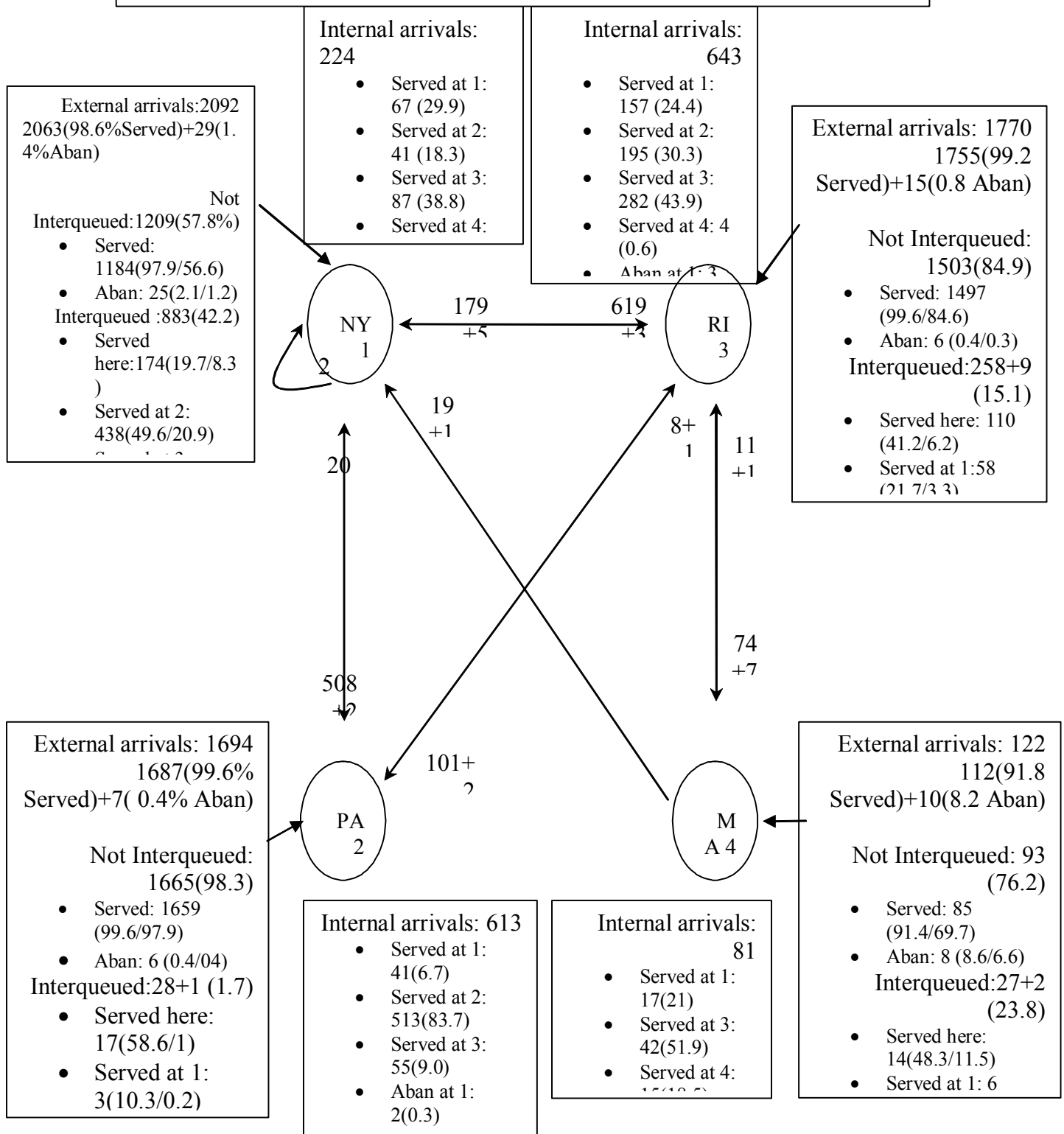
	RG1	RG2	RG3
VRU Target	70% of calls	85% of calls	90% of calls
Abandonment rate	< 1%	< 5%	< 9%
Speed of Answer	100% in 2 rings	80% in 20 seconds	50% in 20 seconds
Average Talk Time	no limit	4 min. average	2 min. average
Rep. Training	universal	product experts	basic product
Rep. Personalization	request rep / callback	FCFS	FCFS
Trans. Confirmation	call / fax	call / mail	mail
Problem Resolution	during call	within 2 business days	within 8 business days

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Distributed Call Center: Member1

10 AM – 11 AM (03/19/01): Interflow Chart Among the 4 Call



Workforce Management: Hierarchical Operational View

Forecasting Customers: Statistics, Time-Series
Agents : HRM (Hire, Train; Incentives, Careers)

Staffing: Queueing Theory

Service Level, Costs

FTE's (Seats)
per unit of time

Shifts: IP, Combinatorial Optimization; LP

Union constraints, Costs

Shift structure

Rostering: Heuristics, AI (Complex)

Individual constraints

Agents Assignments

Skills-based Routing: Stochastic Control

An Introduction to Skills-Based Routing **and its Operational Complexities**

By Ofer Garnett and Avishai Mandelbaum
Technion, ISRAEL

(**Full** Version)

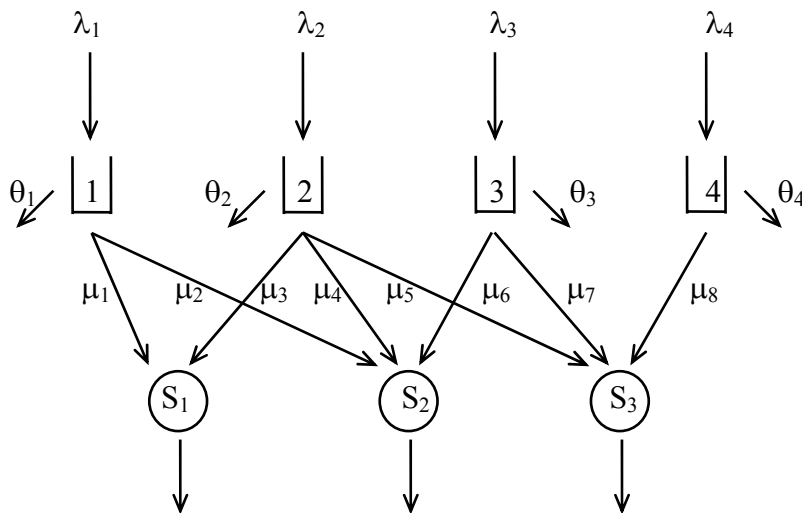
Contents:

- 1. Introduction**
- 2. N-design with single servers**
- 3. X-design with multi-server pools and impatient customers**
- 4. Technical Appendix: Simulations – the computational effort**

Acknowledgement: This teaching-note was written with the financial support of the Fraunhofer IAO Institute in Stuttgart, Germany. The authors are grateful to Dr. Thomas Meiren and Prof. Klaus-Peter Fährnich of the IAO for their assistance and encouragement.

Introduction

Multi-queue parallel-server system = schematic depiction of a **telephone call-center**:



Here the λ 's designate arrival rates, the μ 's service rates, the θ 's abandonment rates, and the S's are the number of servers in each server-pool.

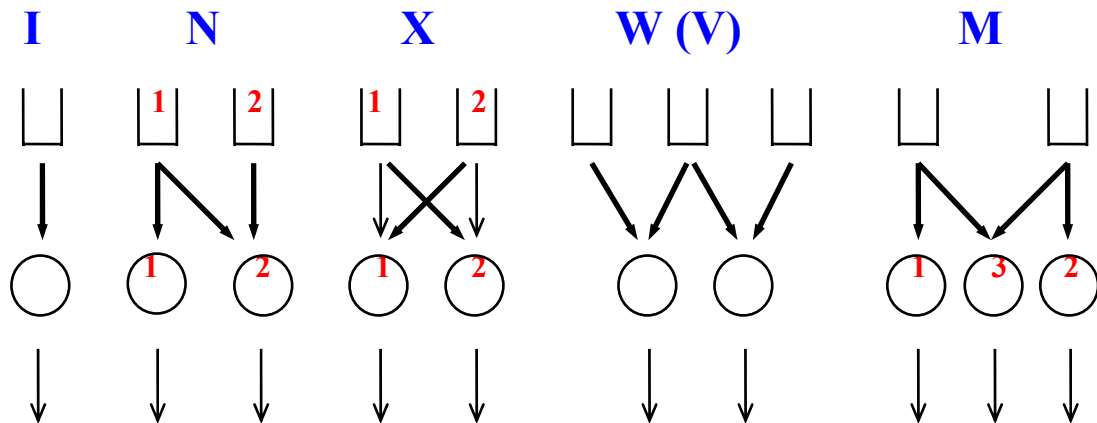
Skills-Based Design:

- **Queue**: "customer-type" requiring a specific type of service;
- **Server-Pool**: "skills" defining the service-types it can perform;
- **Arrow**: leading into a server-pool define its skills / constituency.

For example, a server with skill 2 (**S2**) can serve customers of type 3 (**C3**) at rate μ_6 customers/hour.

Customers of type 3 arrive randomly at rate λ_3 customers/hour, equipped with an impatience rate of θ_3 .

Some Canonical Designs - Animation



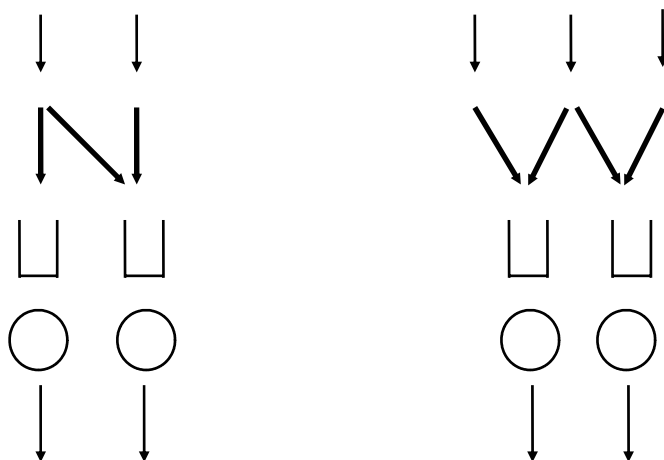
I – dedicated (specialized) agents

N: for example,

- C1 = VIP, then S2 are serving C1 to improve service level.
- C2 = VIP, then S2 serve C1 to improve efficiency.
- S2 = Bilingual.

X: for example, S1 has C1 as Primary and C2 as Secondary Types.

V: Pure Scheduling; **Upside-down V**: Pure Routing.



Major **Design / Engineering** Decisions

1. Classifying customers into **types** (**Marketing**):
Tech. support vs. Billing, VIP vs. Members vs. New
2. Determining server **skills, incentives, numbers** (**HRM, OM, OR**)
Universal vs. Specialist, Experienced / Novice, Uni- / Multi-lingual
3. Prerequisite Infrastructure - MIS / IT / Data-Bases (**CS, Statistics**)
CTI, ERP, Data-Mining

Major **Control** Decisions

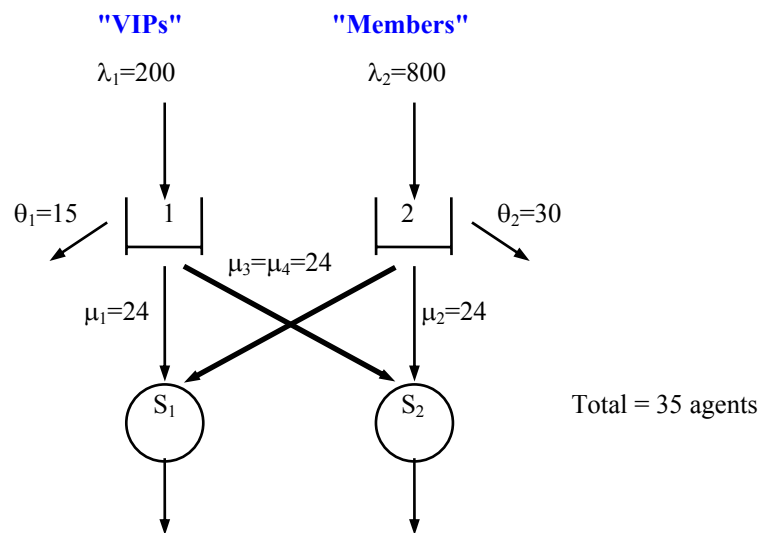
4. Matching customers and agents (**OR**)
 - **Agent Scheduling**: Whenever an agent turns idle and there are queued customers, which customer (if any) should be routed to this agent.
 - **Customer Routing**: Whenever a customer arrives and there are idle agents, which agent (if any) should serve this customer.
5. **Load Balancing**
 - Routing of customers to distributed call centers (eg. nation-wide)

Multidisciplinary Challenging Research

Skills-Based Routing: protocol for online matching of S's and C's.

- **Prevalent:** Static Priorities of customer types and agent skills
- **Index**-based: Dynamic Priorities via continuous review
- **Threshold**-based: Dynamic Management by Exception
- **Others:** discrete review, credit schemes (SLA), scripts; call backs

Example: **Scripts** for Staffing, Scheduling, Routing



Setup A : (X-design)

"VIP" servers : $S_1 = 20$

- If "VIP" queue not empty serve the "VIP" queue + all "Members" waiting more than **40** seconds, as a single FIFO queue.
- If "VIP" queue is empty, serve the first in the "Member" queue.

"Member" servers : $S_2 = 15$

- If "Member" queue not empty serve the "Member" queue + all "VIPs" waiting more than **6** seconds, as a single FIFO queue.
- If "Member" queue is empty, serve the first in the "VIP" queue.

Setup C : (V-design; feasible since servers are assumed equally skilled.)

Total servers: 35

- Serve as a FIFO queue, but "VIPs" enter the queue with a virtual **15** second wait (i.e. as if they had joined the queue 15 seconds earlier).

Chart 2 : 1000 Calls/hour - ASA

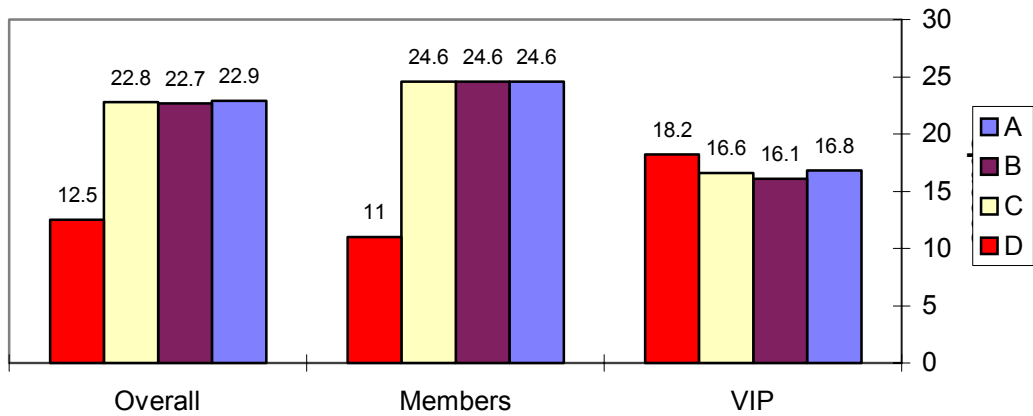


Chart 3 : 1000 Calls - Abandonment

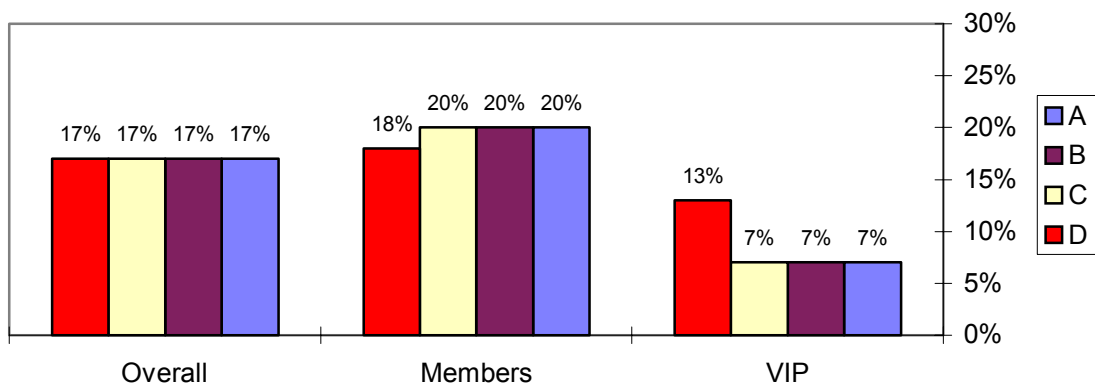
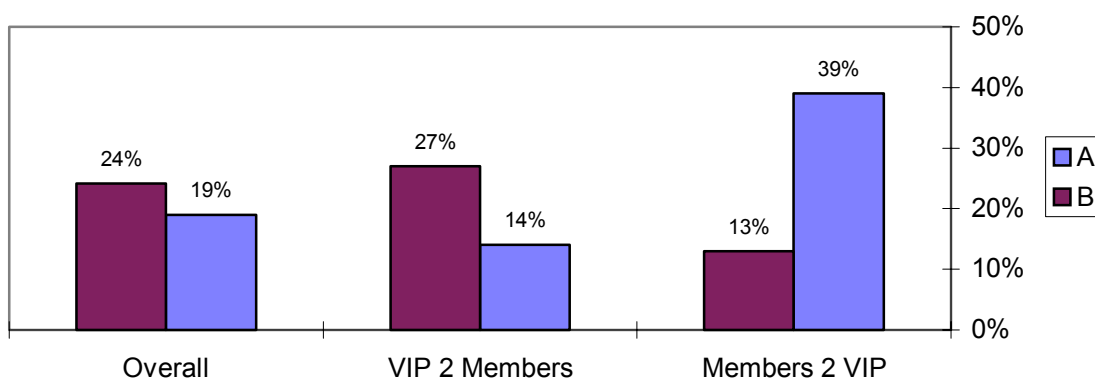


Chart 4 : 1000 Calls - Overflows



WHAT IF : 1500 Calls/hour - ASA

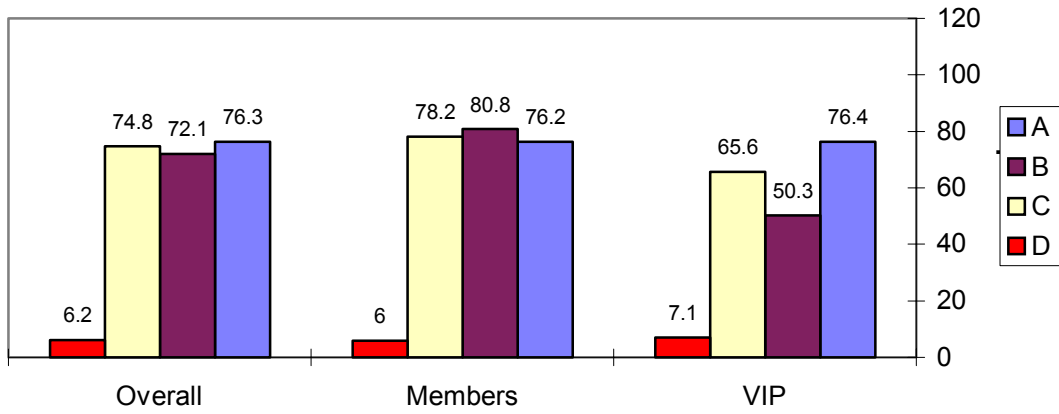


Chart 7 : 1500 Calls - Abandonment

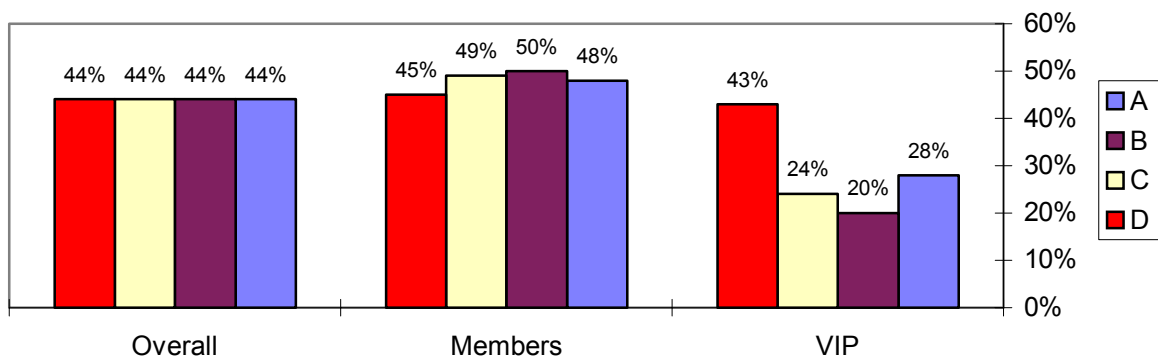
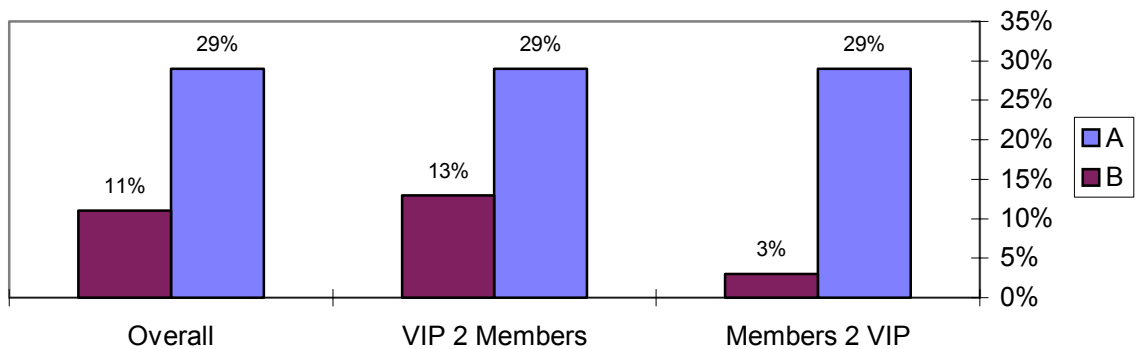


Chart 8 : 1500 Calls - Overflows



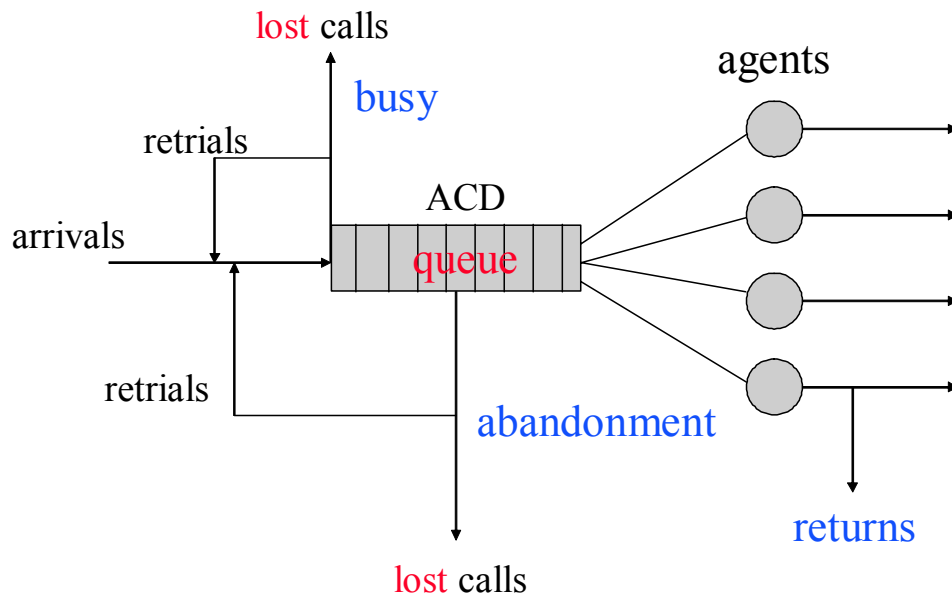
Reality

- Technology enables smart systems
- Reality becomes increasingly complex
- Solutions are urgently needed
- Theory lags significantly behind needs
- Ad-hoc methods: heuristics, simulation-based

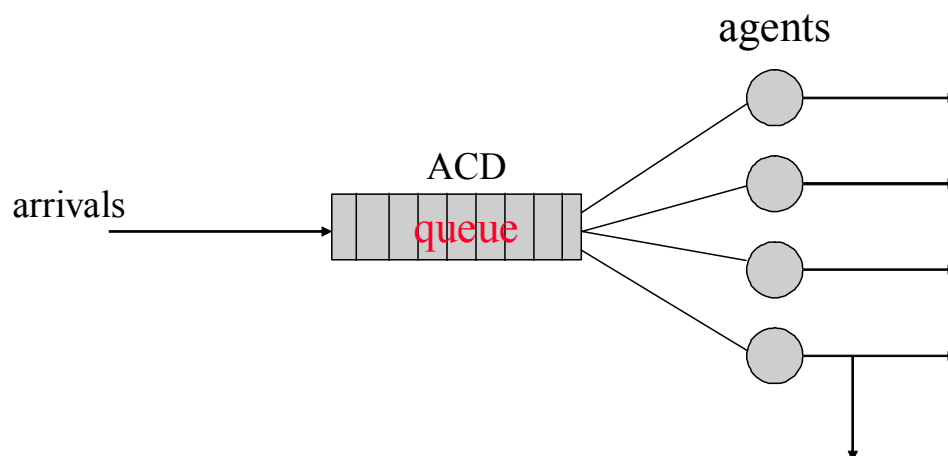
Research Status

- Efficiency-driven SBR well understood and solved
- QED SBR is challenging and advancing
- Small yet significant models for theoretical insight
- Principles/Guidelines for design, staffing, control
- Implementation: fine-tuning of parameters, scale-up

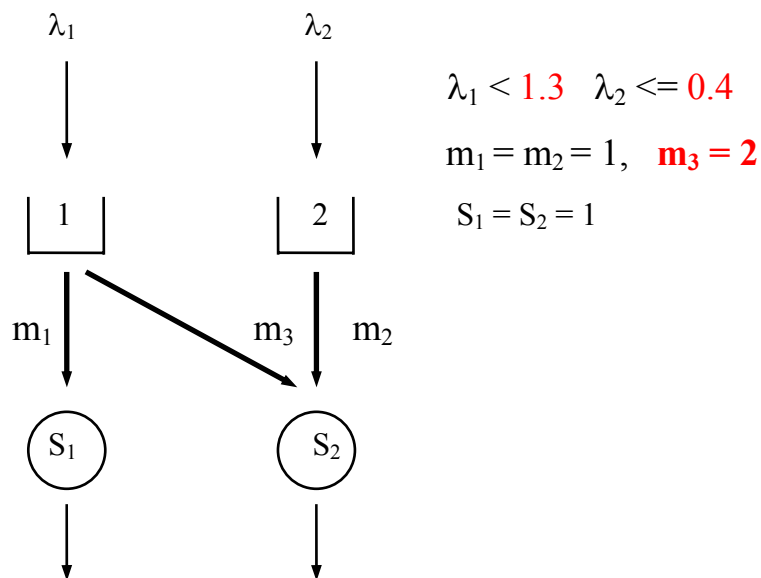
The Basic Call Center



$$\text{Erlang-}C = M/M/N$$

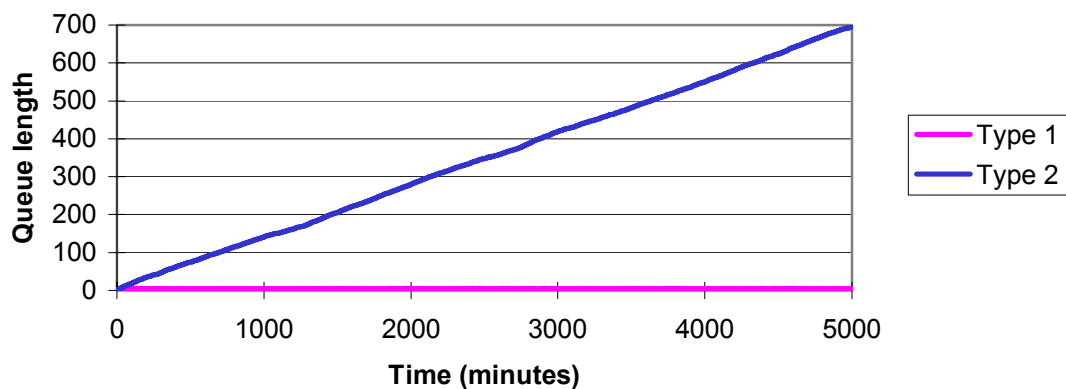


Static Priorities (Cross-Training): Some Subtleties

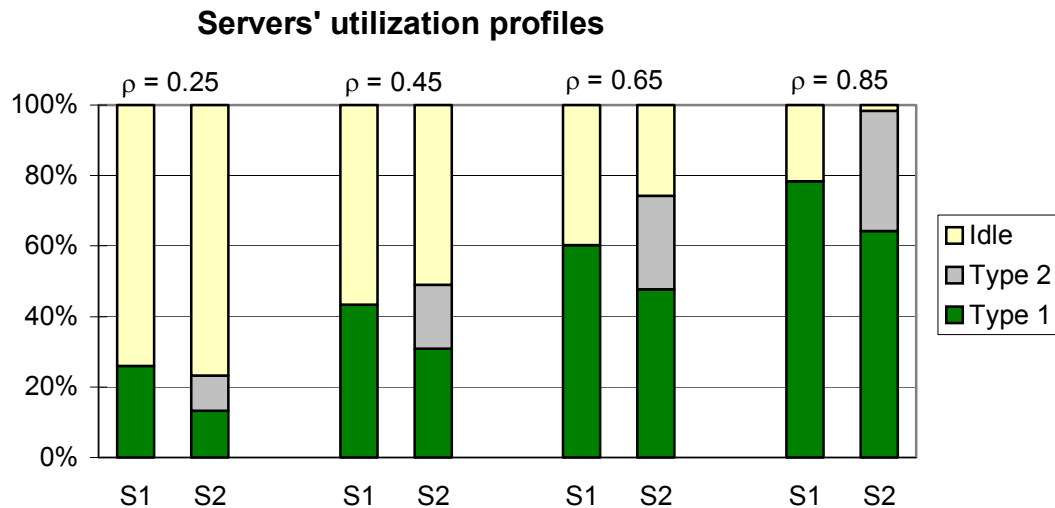


- C_1 are **VIP**, hence S_2 **helps** S_1 by giving priority to C_1 over C_2 .
- If both servers are idle - C_i customers are routed to server S_i

Queue length: S_2 helps with VIP C_1 , Heavy Loading -



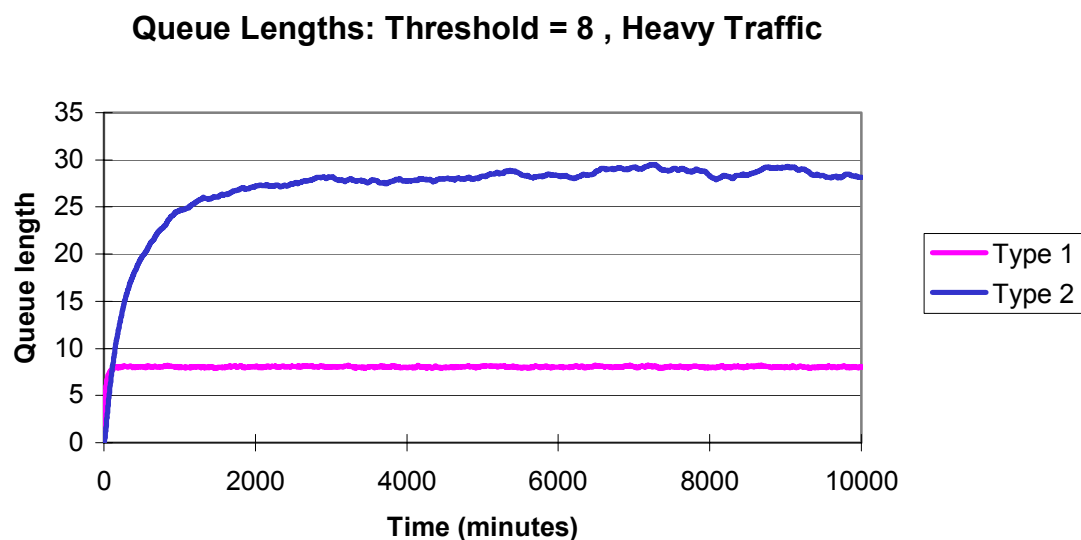
Q_2 "explodes", while Q_1 is negligibly small – why ?



Instability: S2 **overworked** serving C1 and neglecting C2, while S1 is **20%** idle.

To avoid "overzealous help", apply **Threshold control**:

S2 assists S1 **only when Q1 is at or above a certain threshold**



Both Q1 and Q2 are stable.

Now fine-tuning of the threshold value

Efficiency-Driven SBR - the "EASY" Case

Examples: Scarce agents, hence must be well utilized.

Email-dominance, hence can delay response.

Classical **special** case: **V**-design

- **Agent Scheduling**: upon service completion, if
 1. Same mean service times: serve the costliest queue (largest **c**)
 2. Same delay costs: serve the shortest service (smallest **m**)
 3. Generally: serve the largest **c/m** (= index).

General (N, X, W, M, ...) solution: **Index Control** is optimal

- **Customer Routing**: irrelevant, since essentially all customers wait.
- **Agent Scheduling**: upon service completion, the server chooses the queue with the largest index and serves its "oldest" customer.
- **Index**: marginal waiting-cost per unit of average service-time
(Example: "waiting-time" of "oldest" customer in queue)

However: well-managed telephone services are **not**
(at least should not be) Efficiency-Driven !?

At what cost

Copy of Summary Interval • Order PK

Date: 7/7/97

SpHvSkill: Order PK

Time	Avg Speed	Avg Aban	Avg ACD	Avg ACW	Avg Aban	% ACD	% Ans	Avg Pos	Avg Calls	% Serv	% Aux	% ACD
And	Time	Time	Time	Time	Time	Time	Time	Time	Time	Time	Time	Time
W	1/14	1/14	1/14	1/14	1/14	1/14	1/14	1/14	1/14	1/14	1/14	1/14
Totals	10456	10456	10456	10456	10456	10456	10456	10456	10456	10456	10456	10456
12:00 AM	26	00:02	00:00	00:02	00:02	1	76	51	7	4	51	2
12:30 AM	14	00:03	00:00	00:33	00:33	1	89	52	5	3	48	1
1:00 AM	9	00:00	00:00	04:54	11:29	0	91	90	1	7	90	0
5:30 AM	0	00:00	00:00			0	0	0	0	0	0	0
6:00 AM	12	00:00	00:00	03:21	00:18	0	21	100	7	2	100	9
6:30 AM	27	00:00	00:00	02:51	00:20	0	32	100	14	2	100	5
7:00 AM	62	00:00	00:00	03:34	00:15	0	38	100	21	3	100	13
7:30 AM	93	00:00	00:00	03:11	00:34	0	36	100	30	3	100	7
8:00 AM	120	00:00	00:00	03:37	00:40	0	39	100	47	3	100	8
8:30 AM	193	00:00	00:00	03:04	00:14	0	44	100	61	3	100	10
9:00 AM	293	00:01	00:00	03:25	00:25	0	54	98	75	4	97	9
9:30 AM	381	00:02	00:00	03:45	00:22	2	60	97	91	4	93	8
10:00 AM	418	00:02	00:01	03:48	00:26	1	63	97	94	4	98	5
10:30 AM	349	00:00	00:00	03:35	00:33	0	52	99	95	4	98	6
11:00 AM	352	00:00	00:00	03:50	00:27	0	51	100	102	3	100	7
11:30 AM	348	00:00	00:00	03:44	00:18	0	49	100	97	4	100	8
12:00 PM	354	00:01	00:00	03:59	00:18	0	52	95	95	4	95	8
12:30 PM	336	00:00	00:00	03:38	00:21	0	52	99	97	3	99	9
1:00 PM	347	00:00	00:00	03:53	00:32	0	51	99	98	4	99	11
1:30 PM	368	00:00	00:00	03:52	00:14	0	56	98	98	4	99	11
2:00 PM	393	00:01	00:00	03:55	00:17	0	51	100	108	4	100	10
2:30 PM	403	00:00	00:00	03:58	00:13	0	54	100	112	4	100	10
3:00 PM	410	00:00	00:00	04:02	00:15	1	57	98	110	4	98	8
3:30 PM	347	00:00	00:00	03:59	00:14	0	50	100	100	3	100	7
4:00 PM	382	00:00	00:00	03:48	01:37	0	54	100	98	4	100	8
4:30 PM	379	00:00	00:00	03:41	00:19	0	55	99	97	4	99	8
5:00 PM	411	00:00	00:00	03:53	00:19	0	53	100	109	4	100	8
5:30 PM	387	00:01	00:00	03:58	00:19	0	58	99	98	4	99	10
6:00 PM	371	00:01	00:00	03:28	00:25	1	53	98	91	4	98	9
6:30 PM	280	00:00	00:00	03:26	00:13	0	41	100	90	3	100	8
7:00 PM	299	00:00	00:00	03:24	00:17	0	42	100	78	3	100	9

Page 1 of 2

Rough Performance Analysis

Peak 10:00 – 10:30 a.m., with 100 agents
400 calls
3:45 minutes average service time

Offered load $R = \lambda \times E(S)$
 $= 400 \times 3:45 = 1500 \text{ min./30 min.}$
 $= 50 \text{ Erlangs}$

Occupancy $\rho = R/N$
 $= 50/100 = 50\%$

$\Rightarrow$ **Quality-Driven Operation** (Light-Traffic)

Above: $R = 50$, $N = R + 50$, $\approx$ all served immediately.

Rule of Thumb: $N = \lceil R + \delta R \rceil$, $\delta > 0$ service-grade.

Quality-driven: 100 agents, 50% utilization

⇒ **Can** increase offered load - but **by how much?**

Erlang-C **N=100** **E(S) = 3:45 min.**

λ/hr	ρ	$E(W_q) = \text{ASA}$	% Wait = 0
800	50%	0	100%
1000	62.5%	0	100%
1200	75%	0	99.7%
1400	87.5%	0:02 min.	88%
1500	93.8%	0:15 min.	60%
1550	96.9%	0:48 min.	35%
1580	98.8%	2:34 min.	15%
1585	99.1%	3:34 min.	12%

⇒ **Efficiency-driven Operation** (Heavy Traffic)

Above: $R = 99$, $N = R + 1$, $\approx$ all delayed.

Rule of Thumb: **$N = \lceil R + \gamma \rceil$** , $\gamma > 0$ service grade.

Changing N (Staffing)

$$E(S) = 3:45$$

λ/hr	N	OCC	ASA	% Wait = 0
1585	100	99.1%	3:34	12%
1599	100	99.9%	59:33	0%
1599	100+1	98.9%	3:06	13%
1599	102	98.0%	1:24	24%
1599	105	95.2%	0:23	50%

⇒ **New Rationalized Operation**

Heavy traffic, in the sense that $\text{OCC} > 95\%$;

Light traffic, 50% answered immediately

QED Regime = Quality- and Efficiency-Driven Regime

Above: $R = 100$, $N = R + 5$, 50% delayed.

Safety-Staffing $N = \lceil R + \beta \sqrt{R} \rceil$, $\beta > 0$.

Rules of Thumb: Operational Regimes

$R = \lambda \times E(S)$ units of work per unit of time (load)

Efficiency-driven (%{Wait > 0} $\rightarrow$ 100%)

$$N = \lceil R + \gamma \rceil, \quad \gamma > 0 \quad \text{service grade}$$

Quality-driven (%{Wait > 0} $\rightarrow$ 0)

$$N = \lceil R + \delta R \rceil, \quad \delta > 0$$

QED Regime (%{Wait > 0} $\rightarrow \alpha$, $0 < \alpha < 1$)

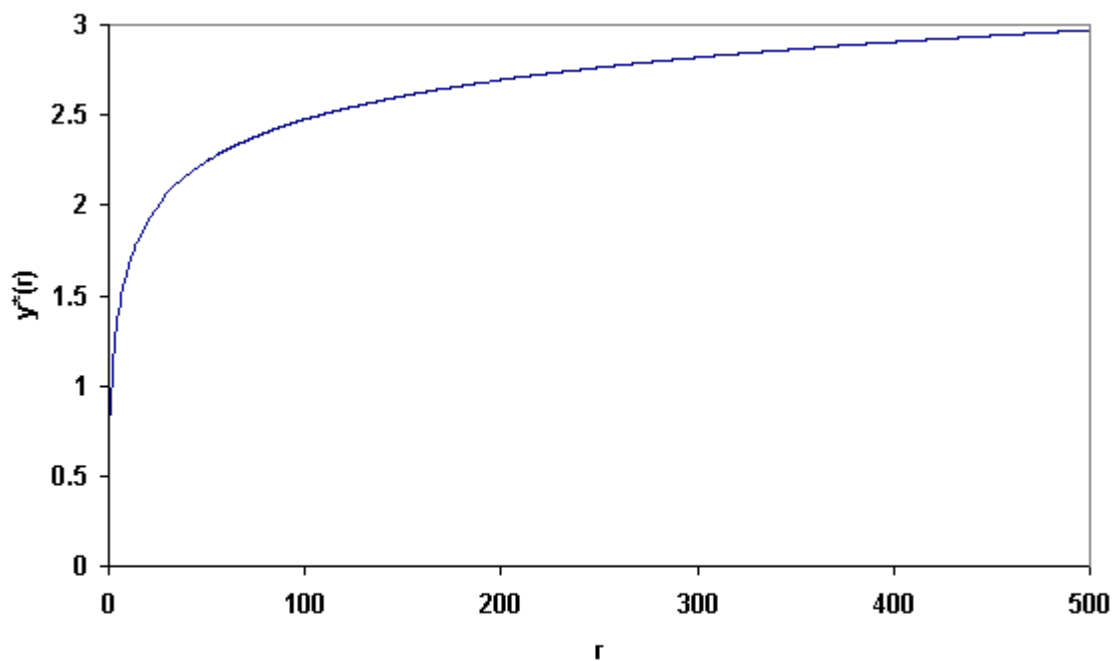
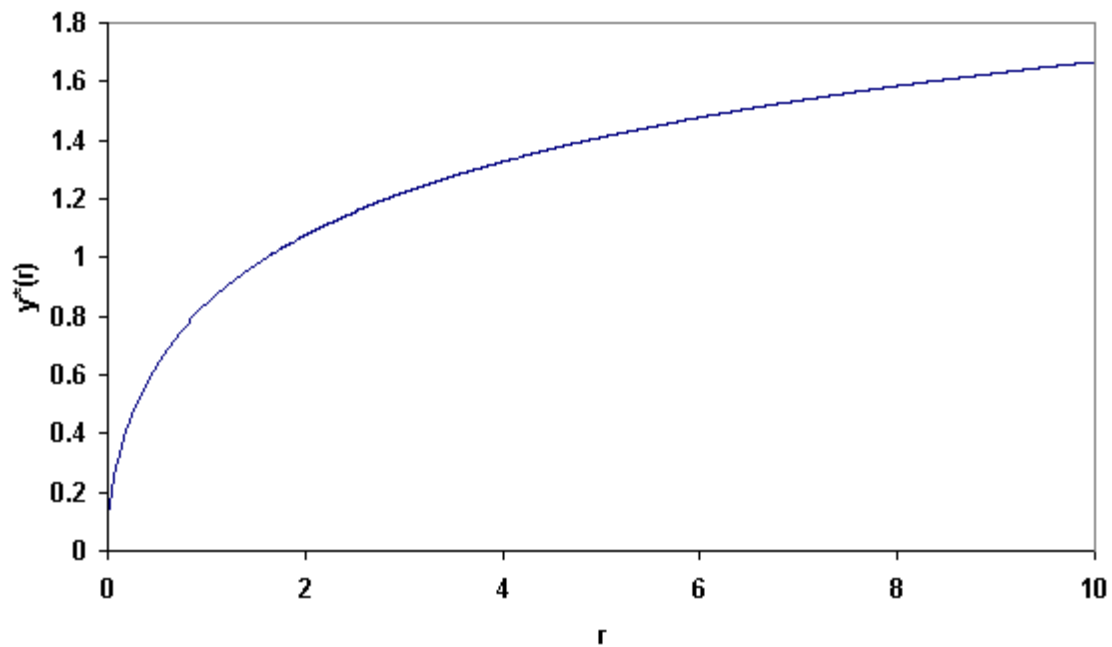
$$N = \lceil R + \beta \sqrt{R} \rceil, \quad \beta > 0 \quad \sqrt{\cdot} \text{ Safety-Staffing}$$

Determine Regimes (Strategy), Parameters (Economics)

Strategy: Managers, Agents (Unions), Customers

Economics: Minimize agent salaries + waiting cost

Square-Root Safety Staffing: $N = R + y^*(r)\sqrt{R}$
 r = cost of delay (1-800) / cost of staffing (salary)



QED Relevance: Member2

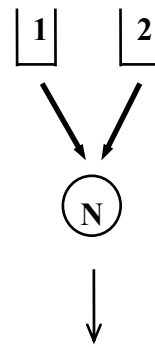
6/13/00 - Tue

Time	Recvd	Answ	Abn %	ASA	AHT	Occ %	On Prod%	On Prod FTE	Sch Open FTE	Sch Avail %
Total	20,577	19,860	~3.0%	30	307	95.1%	85.4%	222.7	234.6	95.0%
8:00	332	308	7.2%	27	302	87.1%	79.5%	59.3	66.9	88.5%
8:30	653	615	5.8%	58	293	96.1%	81.1%	104.1	111.7	93.2%
9:00	866	796	8.1%	63	308	97.1%	84.7%	140.4	145.3	96.6%
9:30	1,152	1,138	1.2%	21	303	90.8%	81.6%	211.1	221.3	95.4%
10:00	1,330	1,286	3.3%	22	307	98.4%	84.3%	223.1	229.0	97.4%
10:30	1,364	1,338	1.9%	33	296	99.0%	84.1%	222.5	227.9	97.6%
11:00	1,380	1,280	7.2%	34	306	98.2%	84.0%	222.0	223.9	99.2%
11:30	1,272	1,247	2.0%	44	298	94.6%	82.8%	218.0	233.2	93.5%
12:00	1,179	1,177	0.2%	1	306	91.6%	88.6%	218.3	222.5	98.1%
12:30	1,174	1,160	1.2%	10	302	95.5%	93.6%	203.8	209.8	97.1%
13:00	1,018	999	1.9%	9	314	95.4%	91.2%	182.9	187.0	97.8%
13:30	1,061	961	9.4%	67	306	100.0%	88.9%	163.4	182.5	89.5%
14:00	1,173	1,082	7.8%	78	313	99.5%	85.7%	188.9	213.0	88.7%
14:30	1,212	1,179	2.7%	23	304	96.6%	86.0%	206.1	220.9	93.3%
15:00	1,137	1,122	1.3%	15	320	96.9%	83.5%	205.8	222.1	92.7%
15:30	1,169	1,137	2.7%	17	311	97.1%	84.6%	202.2	207.0	97.7%
16:00	1,107	1,059	4.3%	46	315	99.2%	79.4%	187.1	192.9	97.0%
16:30	914	892	2.4%	22	307	95.2%	81.8%	160.0	172.3	92.8%
17:00	615	615	0.0%	2	328	83.0%	93.6%	135.0	146.2	92.3%
17:30	420	420	0.0%	0	328	73.8%	95.4%	103.5	116.1	89.2%
18:00	49	49	0.0%	14	180	84.2%	89.1%	5.8	1.4	416.2%

V-Design: Pure Scheduling

N agents, fully flexible

C1 = VIP



Optimal Scheduling: Agent Reservation

- C1(=VIP) always served, if possible;
- C2 served only if # of idle agents exceeds a threshold.

QED regime: $\sqrt{\cdot}$ Safety-Staffing, as before.

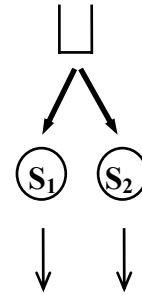
Threshold Size (relative to N) determines Service Levels:

- Large: C1 is Q-served, C2 is E-served
- Small: C1 and C2 indistinguishable QED
- Moderate: C1 is Q-served, C2 is QED

Upside-Down-V Design: Pure Routing

Homogeneous Customers

Heterogeneous Agents: **S1 = Faster**



Optimal Routing: **"Slow-Server"** phenomenon

- S1(=Fast) always employed, if possible;
- S2(= Slow) employed if # in queue exceeds a threshold.

QED regime: $\sqrt{\cdot}$ Safety-Staffing for S1+S2.

- No threshold needed: just have all servers work when possible, ensuring that the "fast" get the priority.
- Can do also detailed staffing: how many S1 and S2.
- Distributed call centers: similar

But N-Design active challenging research

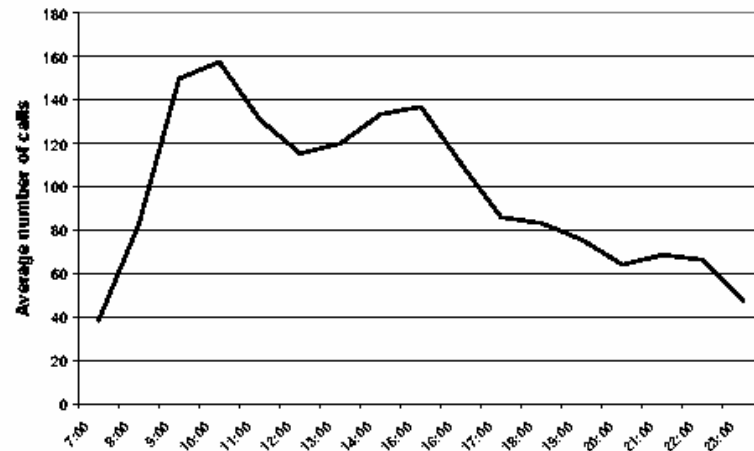
Beyond Erlang-C: (Im)Patience (Erlang_A)

6/13/00 - Tue

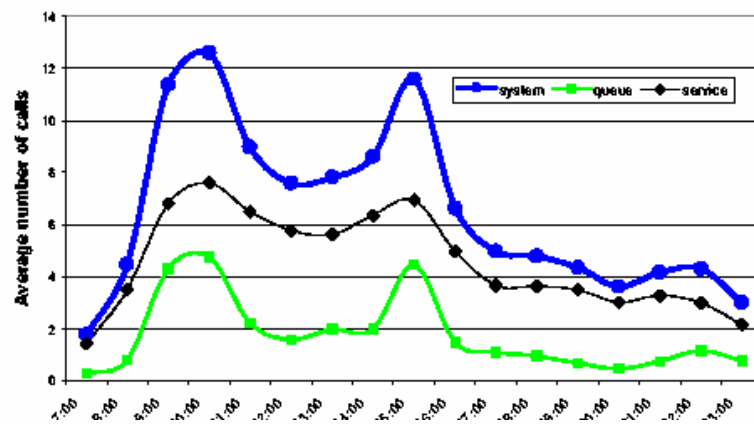
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Beyond Erlang-C: Predictable Variability

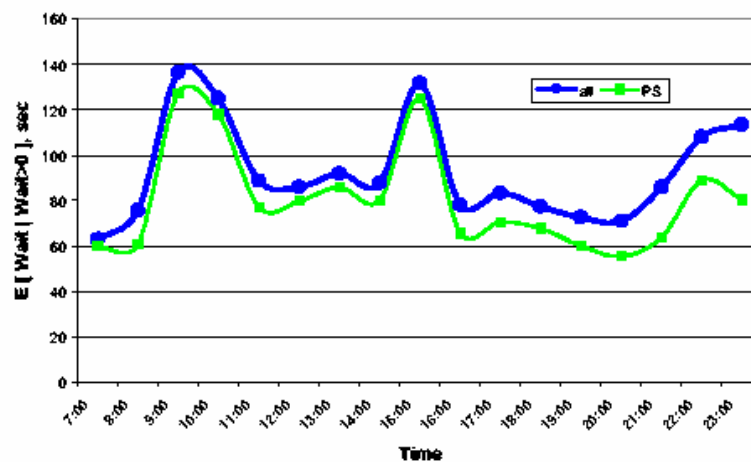
Arrivals



Queues



Waiting



END OF LECTURE

Operational Aspects of Impatience

The "fittest" survive and wait less – much less!

Recall earlier Q, E and QED Scenarios ($E(S) = 3:45$):

λ /hr	N	OCC	ASA	% Wait ≤ 2 sec
1599	100	99.9%	59:33	1%
1599	105	95.2%	0:23	51%
1600	100	100%	<u>infinity</u>	0%
		BUT	with	Impatience
				%Abandonment
1600	100	97.3%	0:23	2.7 %
1600	95	98.4%	0:23	6.5%
1800	105	97.7%	0:23	3.4%

QED with **Impatient** Customers:

Erlang-A: Theoretical performance analysis

Free Internet implementation (4CallCenters.com)

Theorem (Halfin-Whitt '81; Garnett, M. and Reiman '02):

Consider a queue attended by N servers, N "large".

Then the following **points of view** are equivalent:

- **QED** $\% \{\text{Wait} > 0\} \approx \alpha, \quad 0 < \alpha < 1;$
- **Customers** $\% \{\text{Abandon}\} \approx \frac{\gamma}{\sqrt{N}}, \quad 0 < \gamma;$
- **Agents** $\text{OCC} \approx 1 - \frac{\beta}{\sqrt{N}} \quad -\infty < \beta < \infty;$
- **Managers** $N \approx R + \beta \sqrt{R}, \quad R = \lambda \times E(S) \text{ not small};$

QED performance (ASA, ...) is very easily computable, all in terms of β (the square-root safety staffing level).

Covers also the Extremes:

$$\alpha = 1 : N = R - \gamma R$$

Efficiency-driven

$$\alpha = 0 : N = R + \gamma R$$

Quality-driven

Abandonment Important

- Lost business (now)
- Poor service level (future losses)
- 1-800 costs decrease (out-of-pocket vs. alternative)
- Self-selection: the “fittest” survive and wait less
- Must account for (carefully) in models and measures
 - Otherwise wrong picture of reality
 - Misleading performance measures
 - Unstable models (vs. Robustness)

But Abandonment also Interesting & Challenging

- Queueing Science
(Paradigm: experiment, measure, model, validate)
- Research: OR + Psychology + Marketing
(Modelling: steady-state, transient, equilibrium)
- Scope of Applications
 - VRU/IVR: opt-out-rates
 - Internet: business-drivers (60% and more)
 - Call Centers: customer-centric performance measures